

# ULS Verification of Core Walls in Accordance with EN1998-1:2004

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# Content

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## Introduction

- Basic code requirements
- Verification algorithm



## Numerical Example

- Verification of ULS limit states for complexly shaped Core Wall



## Optimization?

- How to improve solutions and what to avoid in practice?



## Conclusions

- Summary of previous chapters



# 1. Introduction

- Focal point will be on core walls as they are the most often used element for lateral stability in mid-rise and high-rise buildings
- Special emphasis is on the verifications of ductility requirements in walls of complex geometry

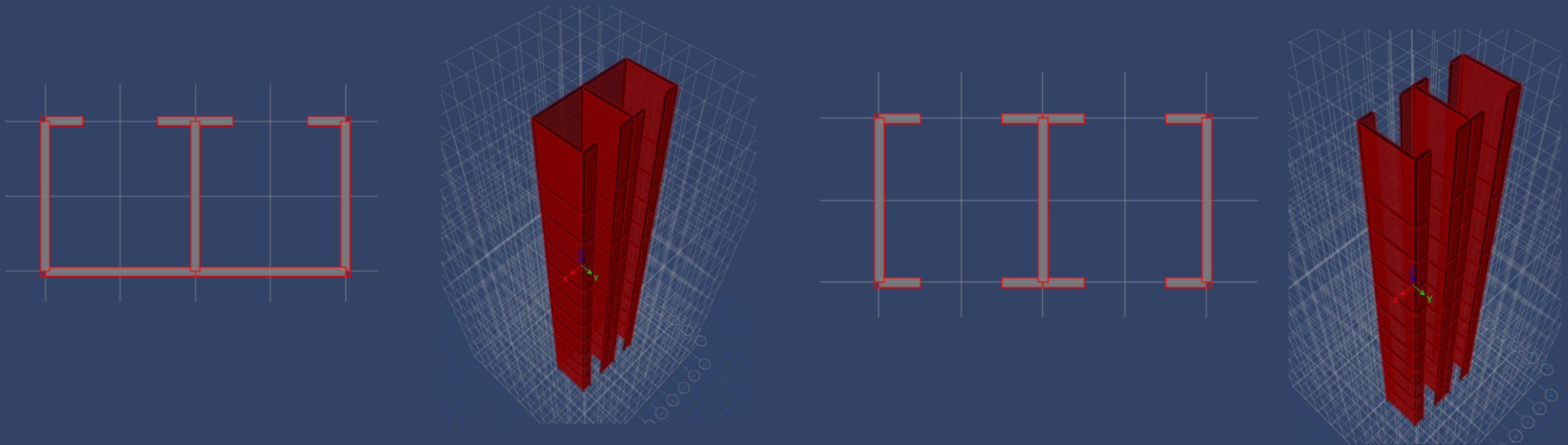


Figure 1: Common shapes of Core Walls

- Important clauses from Code [1]



# 1.1 Basic code requirements [1]

5.2.1 (1) [1]



5.4.3.4.1 (4) [1]

5.4.3.4.2 (5) [1]

Summary

## Ductile wall:

Ductile wall is an element fixed at its base so that the relative rotation of this base with respect to the rest of the structural system is prevented, and that is designed and detailed to dissipate energy *in a flexural plastic hinge zone free of openings or large perforations, just above its base.*



# 1.1 Basic code requirements [1]

5.2.1 (1) [1]



5.4.3.4.1 (4) [1]

5.4.3.4.2 (5) [1]

Summary

## Walls of complex geometry:

Composite wall sections consisting of connected or intersecting rectangular segments (L-, T-, U-, I or similar sections) **should be taken as integral units**, consisting of a web or webs parallel or approximately parallel to the direction of the acting seismic shear force and a flange or flanges normal or approximately normal to it

*\*Effective width of flange should be accounted for*



# 1.1 Basic code requirements [1]

5.2.1 (1) [1]



5.4.3.4.1 (4) [1]

5.4.3.4.2 (5) [1]

Summary

## Length of confinement zone:

For walls with barbells or flanges, or with a section consisting of several rectangular parts (L-, T-, U-, I-shaped sections, etc.) the mechanical volumetric ratio of the confining reinforcement in the boundary elements may be determined as follows:

$$x_u = (v_d + \omega_v) \cdot \frac{l_w \cdot b_c}{b_0}$$

*\*Applicable only for rectangular compressive zone*



# 1.1 Basic code requirements [1]

5.2.1 (1) [1]



5.4.3.4.1 (4) [1]

5.4.3.4.2 (5) [1]

Summary

## How to assess core walls?

- Avoid the problem by designing only rectangular shear walls
- Keep increasing the width of the compressed zone so it remains rectangular
- *Perform more in-depth analysis to determine the actual curvature ductility of the composite core wall section*



# 1.1 Basic code requirements [1]

## Ductility requirements

Goal is to verify that section has sufficient curvature ductility:

$$\mu_{\phi.cap} \geq \mu_{\phi.req}$$

$$\mu_{\phi.req} = \begin{cases} 2 \cdot q_0 - 1, & T_1 \geq T_C \\ 1 + 2 \cdot (q_0 - 1) \cdot \frac{T_C}{T_1}, & T_1 < T_C \end{cases}$$

$$\mu_{\phi.cap} = \frac{\mu_u}{\mu_y}$$

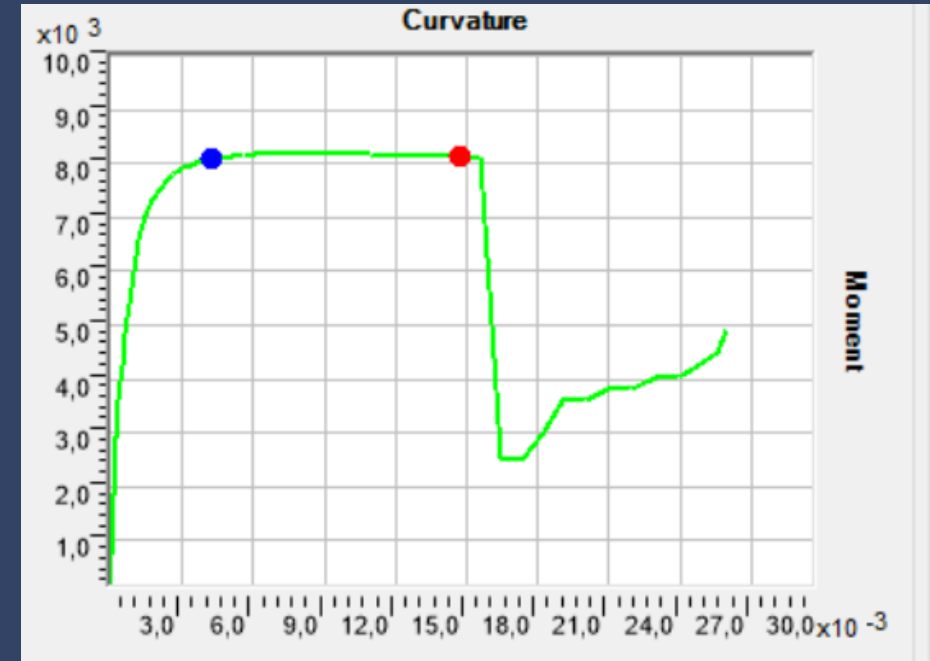


Figure 2: Moment-Curvature Diagram





## 1.2. Verification algorithm [2]

### 1.2.1 Calculate curvature on the onset of yielding $\mu_y$

Section is considered to start yielding when either of criteria is met:



**Expected behaviour in shear walls**

Reinforcement reaches its yield strain  $\varepsilon_{sy}$



**Possible behaviour in members with high axial compression – not expected in shear walls**

Concrete reaches characteristic strain  $\varepsilon_c^*$



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Reinforcement reaches its yield strain  $\varepsilon_{sy} = \frac{f_{yd}}{E_s}$



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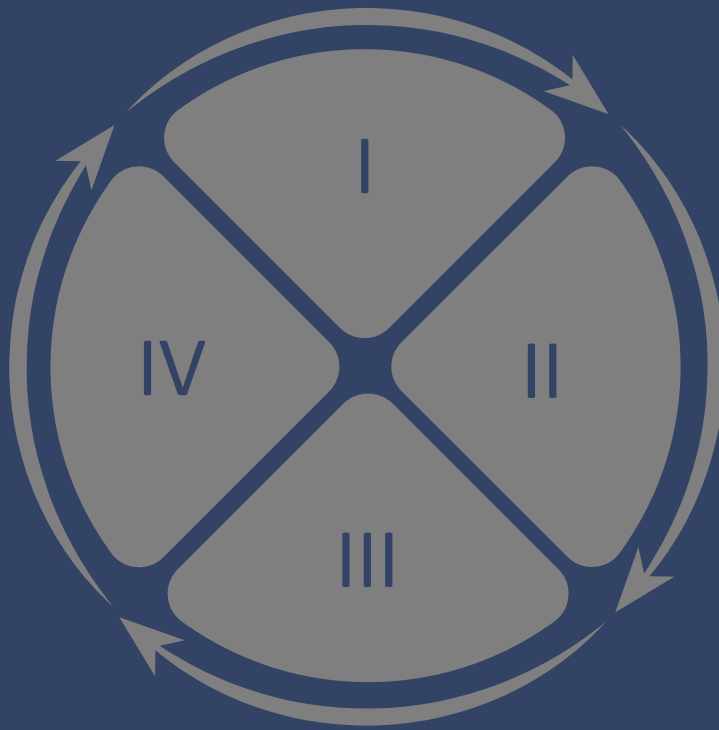
Concrete reaches characteristic strain  $\varepsilon_c^* = 1.8 \cdot \frac{f_c}{E_c}$



## 1.2. Verification algorithm [2]

### 1.2.2 Calculate ultimate curvature $\mu_u$

Section can reach its ultimate curvature in one of four modes:



**Failure before spalling of concrete cover**

Reinforcement reaches its ultimate strain  $\varepsilon_{su}$



**Failure before spalling of concrete cover**

Unconfined concrete reaches its ultimate strain  $\varepsilon_{cu}$



**Failure after spalling of concrete cover**

Reinforcement reaches its ultimate strain  $\varepsilon_{su}$



**Failure after spalling of concrete cover**

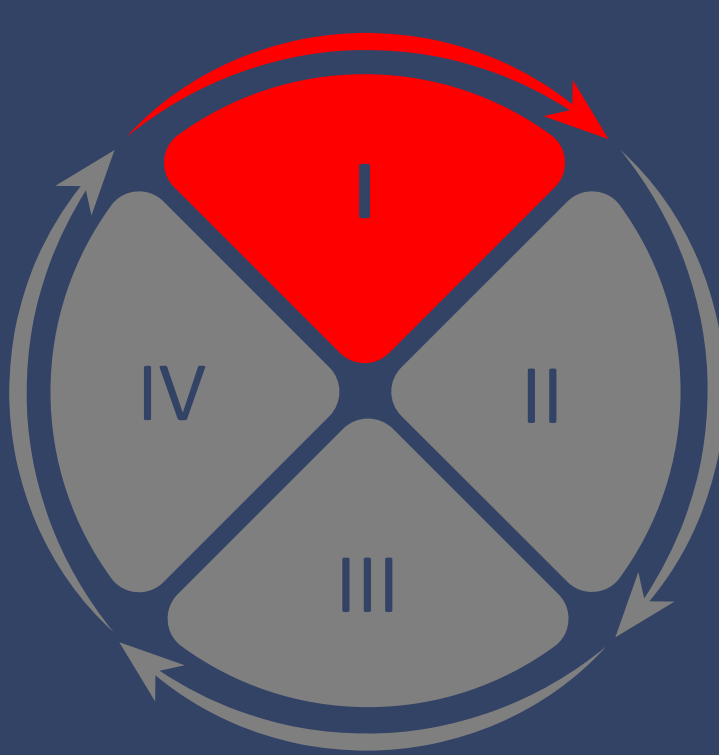
Confined concrete reaches its ultimate strain  $\varepsilon_{cu.c}$



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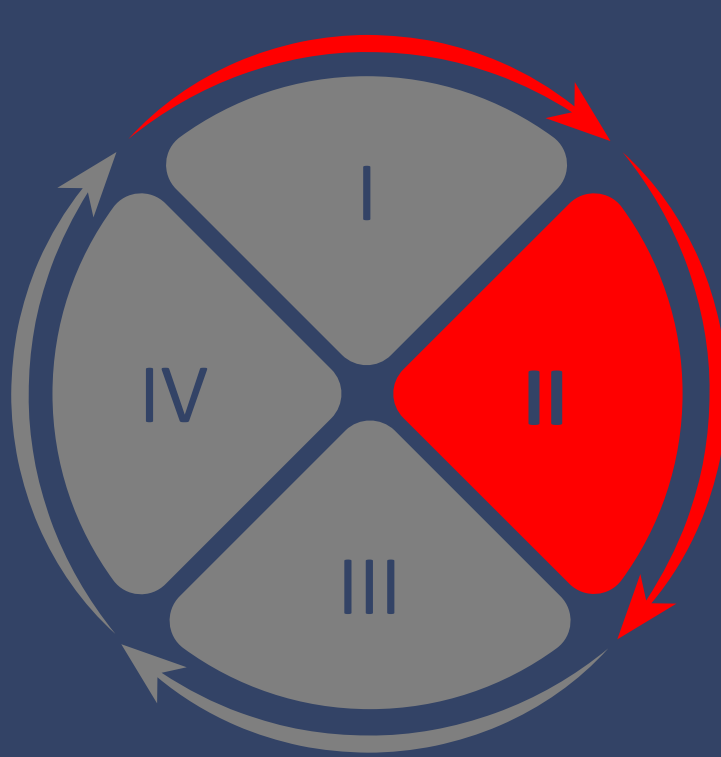
Confined concrete reaches its ultimate strain  $\varepsilon_{cu.c}$



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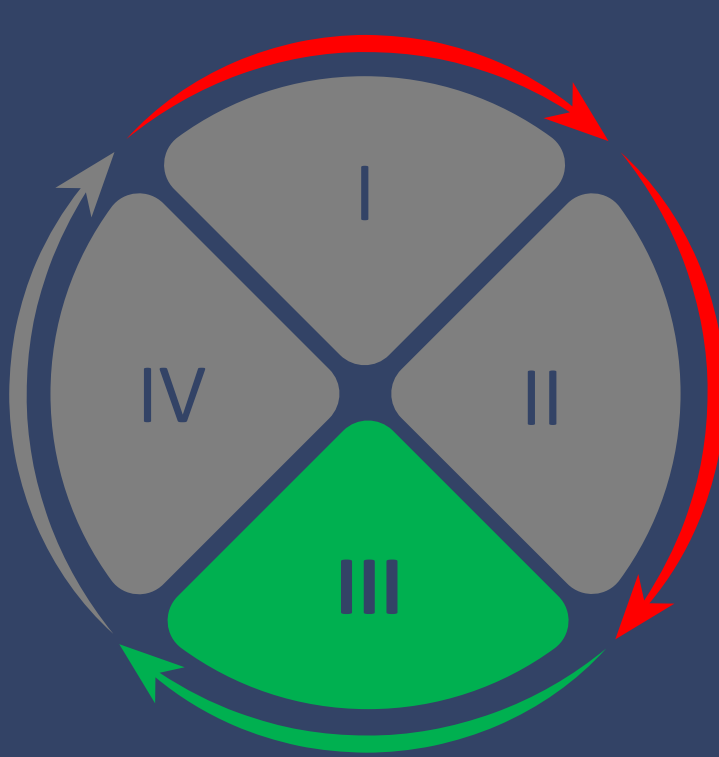
Confined concrete reaches its ultimate strain  $\varepsilon_{cu.c}$



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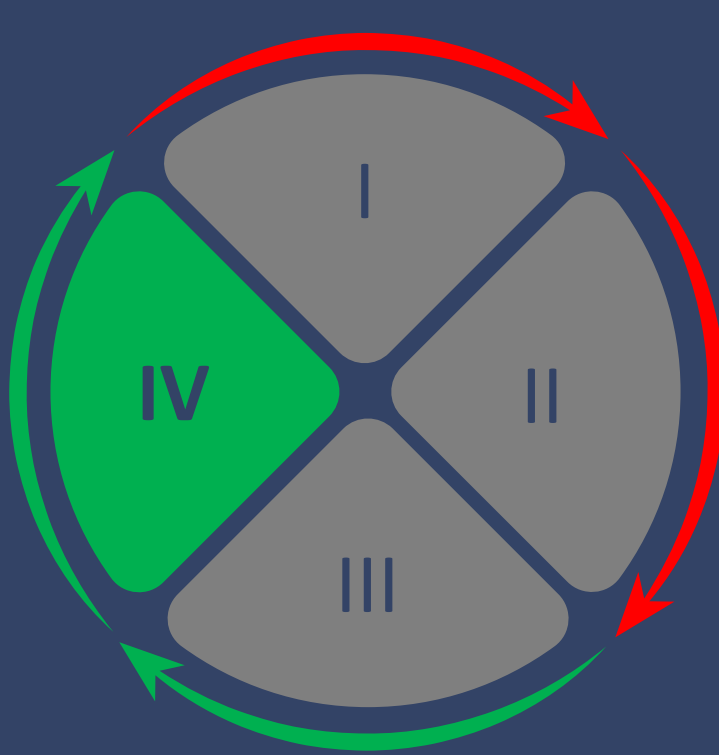
Confined concrete reaches its ultimate strain  $\varepsilon_{cu.c}$



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Reinforcement reaches its ultimate strain  $\varepsilon_{su}$



**Failure before spalling of concrete cover**

Unconfined concrete reaches its ultimate strain  $\varepsilon_{cu}$



**Failure after spalling of concrete cover**

Reinforcement reaches its ultimate strain  $\varepsilon_{su}$



**Failure after spalling of concrete cover**

Confined concrete reaches its ultimate strain  $\varepsilon_{cu.c}$





## 2. Numerical example

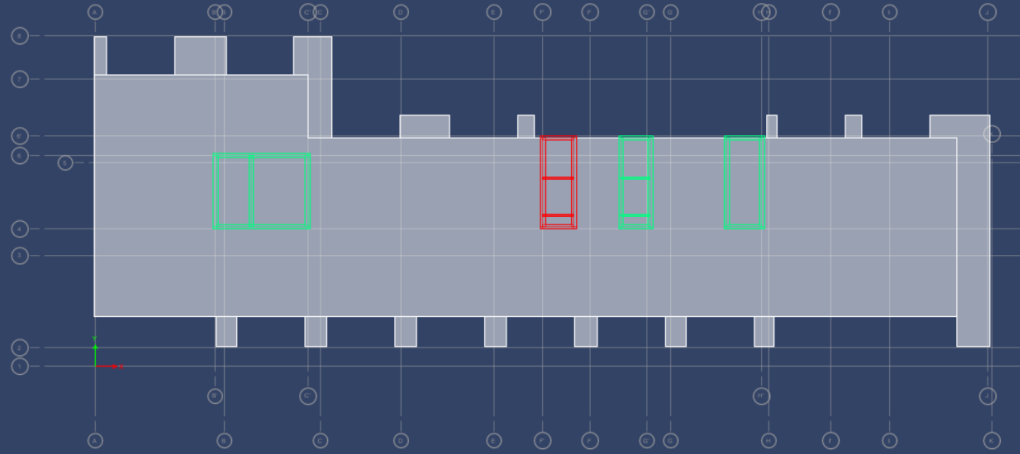


Figure 3: Analyzed core wall in plan view

Height	84m
Stories	23
$q_0$	2
Concrete	C50/60
Reinforcement	B500B
$T_f$	3s
$T_c$	0,5s

Ductility class	DCM
$a_g/g$	0,10

Table 1: Basic structure properties

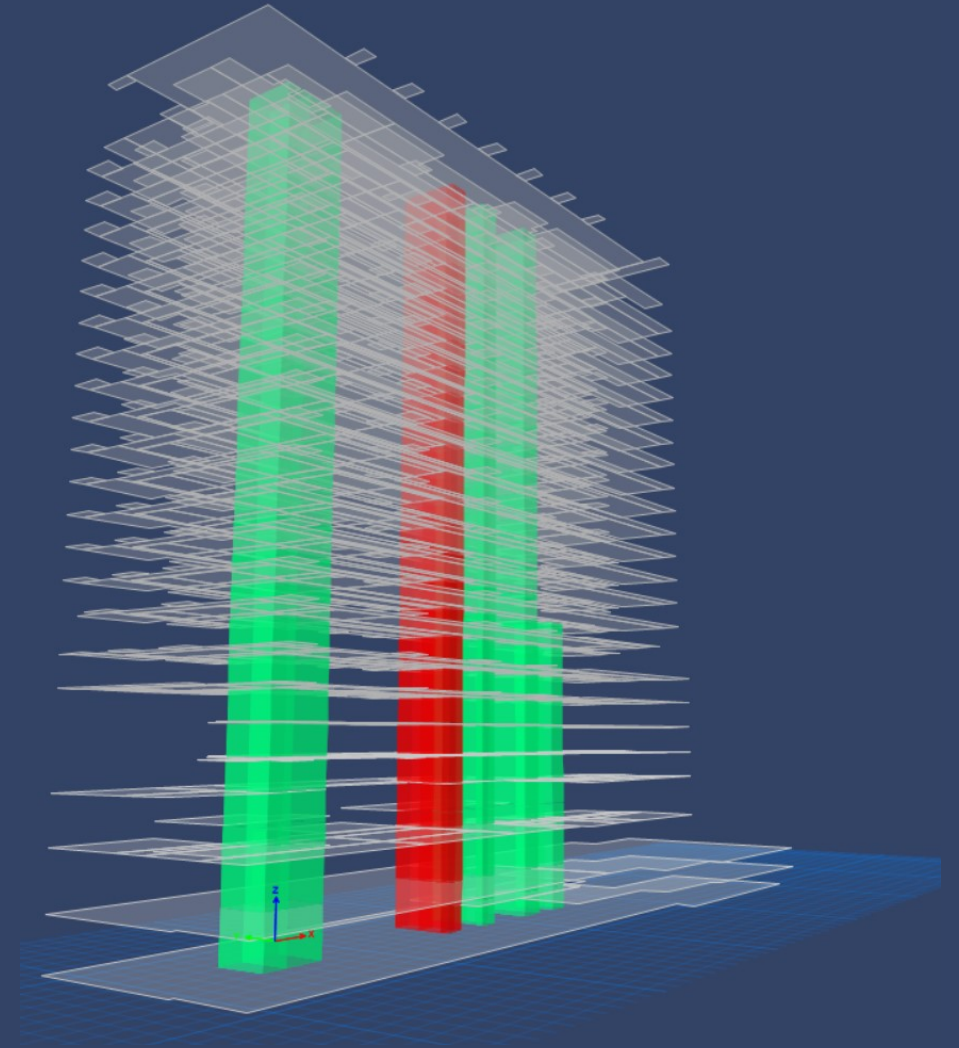


Figure 4: Analyzed core wall in isometric view



## 2. Numerical example

### 2.1. Core wall as an assemblage of independent shear walls?

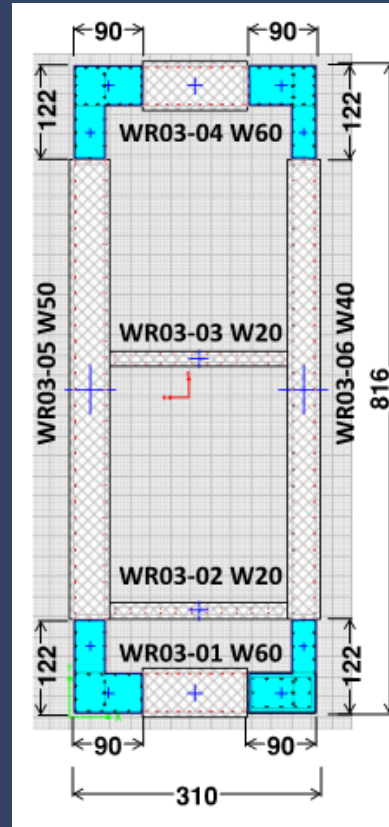


Figure 5: Confined zones and dimensions of core wall



## 2. Numerical example

### 2.1. Core wall as an assemblage of independent shear walls?

Comment	Wall	Combo	$l_w$ [m]	$b_w$ [m]	$N_{ed}$ [kN]	$v$	Web RFT		Confined RFT		$M_{ed}$ [kNm]	$M_{Rd}$ [kNm]	$M_{Ed}/M_{Rd}$ [%]	$l_{c,geo}$ [m]	$l_{c,calc}$ [m]	$l_{c,adp}$ [m]	Comment
Governing	WR03-01	MAX	3,10	0,60			12	150	16	200			29,23				
Seismic Combo	WR03-01	Nmax S	3,10	0,60	18000	0,34	12	150	16	200	1500	22687	6,61	0,90	0,90	0,90	Minimal geometrical length
	WR03-01	Nmin S	3,10	0,60	100	0,00	12	150	16	200	1500	5132	29,23	0,90	0,90	0,90	
	WR03-01	Tension Force S	3,10	0,60	0	0,00	12	150	16	200	0	0	0,00	-	-	-	
Governing	WR03-04	MAX	3,10	0,60			12	150	16	150			83,59				
Seismic Combo	WR03-04	Nmax S	3,10	0,60	15500	0,29	12	150	16	150	1600	22193	7,21	0,90	0,90	0,90	Minimal geometrical length
	WR03-04	Nmin S	3,10	0,60	14000	0,27	12	150	16	150	1600	21139	7,57	0,90	0,90	0,90	
	WR03-04	Tension Force S	3,10	0,60	-3200	-0,06	12	150	16	150	1600	1914	83,59	-	-	-	
Governing	WR03-05	MAX	8,16	0,50			12	200	16	200			54,43				
Seismic Combo	WR03-05	Nmax S	8,16	0,50	24200	0,21	12	200	16	200	33000	97361	33,89	1,22	1,22	1,22	Minimal geometrical length
	WR03-05	Nmin S	8,16	0,50	11000	0,10	12	200	16	200	33000	60631	54,43	1,22	1,22	1,22	
	WR03-05	Tension Force S	8,16	0,50	0	0,00	12	200	16	200	0	0	0,00	-	-	-	
Governing	WR03-06	MAX	8,16	0,40			12	200	16	200			49,30				
Seismic Combo	WR03-06	Nmax S	8,16	0,40	17000	0,18	12	200	16	200	22000	75270	29,23	1,22	1,22	1,22	Minimal geometrical length
	WR03-06	Nmin S	8,16	0,40	6400	0,07	12	200	16	200	22000	44626	49,30	1,22	1,22	1,22	
	WR03-06	Tension Force S	8,16	0,40	0	0,00	12	200	16	200	0	0	0,00	-	-	-	

Table 2: Verification of constituent walls as independent shear walls

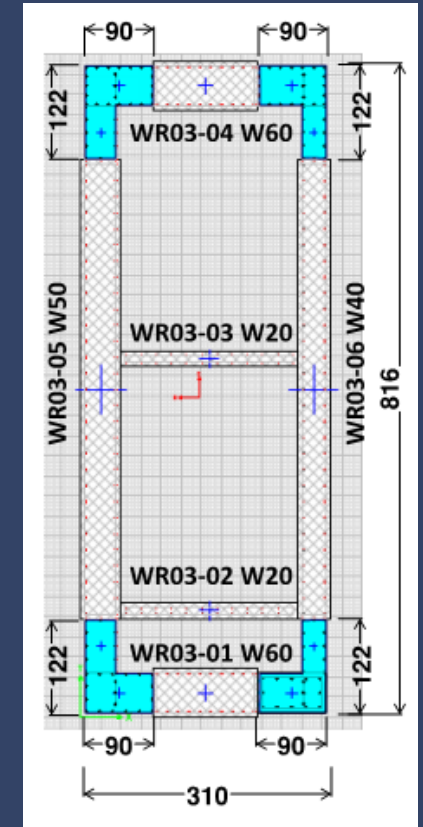


Figure 5: Confined zones and dimensions of core wall



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Seismic Combo	WR03-01	Nmax S	3,10	0,60	18000	0,34	12	Minimal reinforcement		200	1500	22687	6,61	0,90	0,90	0,90	
	WR03-01	Nmin S	3,10	0,60	100	0,00	12			200	1500	5132	29,23	0,90	0,90	0,90	
	WR03-01	Tension Force S	3,10	0,60	0	0,00	12	150	16	200	0	0	0,00	-	-	-	
Governing	WR03-04	MAX	3,10	0,60			12	150	16	150			83,59				Minimal length of boundary zone
Seismic Combo	WR03-04	Nmax S	3,10	0,60	15500	0,29	12	Almost minimal reinforcement		150	1600	22193	7,21	0,90	0,90	0,90	
	WR03-04	Nmin S	3,10	0,60	14000	0,27	12			150	1600	21139	7,57	0,90	0,90	0,90	
	WR03-04	Tension Force S	3,10	0,60	-3200	-0,06	12	150	16	150	1600	1914	83,59	-	-	-	
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Governing	WR03-06	MAX	8,16	0,40			12	200	16	200			49,30				Minimal length of boundary zone
Seismic Combo	WR03-06	Nmax S	8,16	0,40	17000	0,18	12	Minimal reinforcement		200	22000	75270	29,23	1,22	1,22	1,22	
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	WR03-06	Tension Force S	8,16	0,40	0	0,00	12	200	16	200	0	0	0,00	-	-	-	

Table 2: Verification of constituent walls as independent shear walls

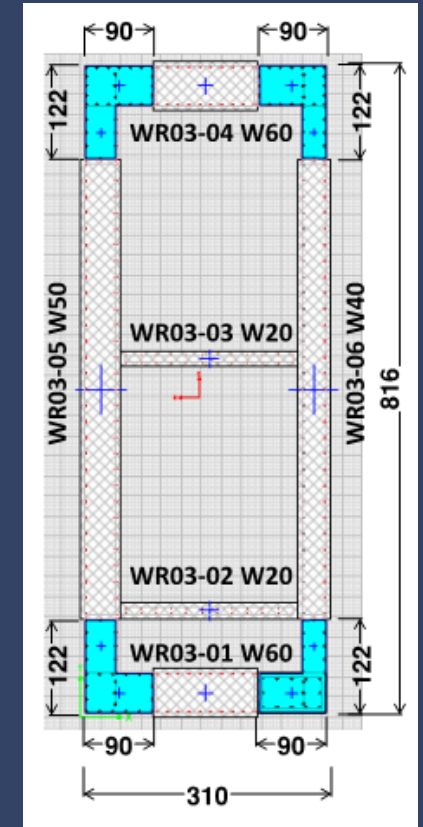


Figure 5: Confined zones and dimensions of core wall



## 2. Numerical example

### 2.1. Core wall as an assemblage of independent shear walls?

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Seismic Combo	WR03-01	Nmax S	3,10	0,60	18000	0,34	12	Minimal		200	1500	22687	6,61	0,90	0,90	0,90	
	WR03-01	Nmin S	3,10	0,60	100	0,00	12	reinforcement		200	1500	5132	29,23	0,90	0,90	0,90	
	WR03-01	Tension Force S	3,10	0,60	0	0,00	12	150	16	200	0	0	0,00	-	-	-	
Governing	WR03-04	MAX	3,10	0,60			12	Almost		150			83,59				Minimal length of boundary zone
Seismic Combo	WR03-04	Nmax S	3,10	0,60	15500	0,29	12	minimal		150	1600	22193	7,21	0,90	0,90	0,90	
	WR03-04	Nmin S	3,10	0,60	14000	0,27	12	reinforcement		150	1600	21139	7,57	0,90	0,90	0,90	
	WR03-04	Tension Force S	3,10	0,60	-3200	-0,06	12	150	16	150	1600	1914	83,59	-	-	-	
Governing	WR03-05	MAX	8,16	0,50			12	200	16	200			54,43				Minimal length of boundary zone
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	WR03-05	Nmin S	8,16	0,50	11000	0,10	12	reinforcement		200	33000	60631	54,43	1,22	1,22	1,22	
	WR03-05	Tension Force S	8,16	0,50	0	0,00	12	200	16	200	0	0	0,00	-	-	-	
Governing	WR03-06	MAX	8,16	0,40			12	200	16	200			49,30				Minimal length of boundary zone
Seismic Combo	WR03-06	Nmax S	8,16	0,40	17000	0,18	12	Minimal		200	22000	75270	29,23	1,22	1,22	1,22	
	WR03-06	Nmin S	8,16	0,40	6400	0,07	12	reinforcement		200	22000	44626	49,30	1,22	1,22	1,22	
	WR03-06	Tension Force S	8,16	0,40	0	0,00	12	200	16	200	0	0	0,00	-	-	-	

Table 2: Verification of constituent walls as independent shear walls

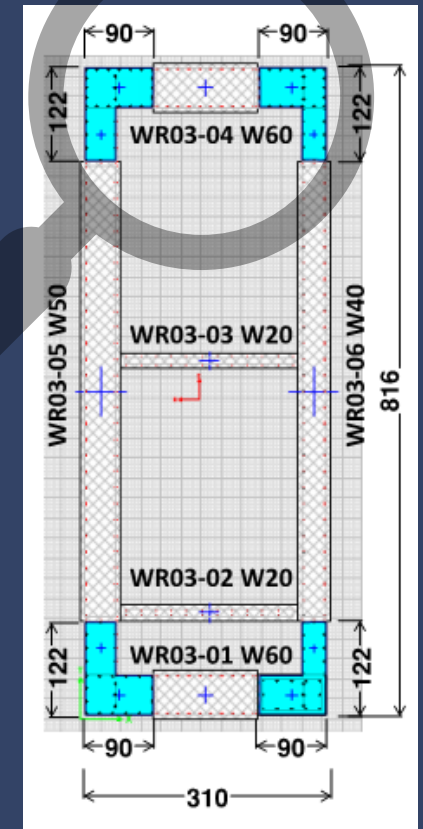


Figure 5: Confined zones and dimensions of core wall





## 2. Numerical example

### 2.2. Core wall as an integral element

Global analysis Tower			
$M_{2,max}$	$M_{2,min}$	$M_{3,max}$	$M_{3,min}$
[kNm]	[kNm]	[kNm]	[kNm]
16500	-31000	138000	-99500
Axial force [kN]			
$N_{max,c}$	-55000	$N_{min,c}$	-40000

Table 3: Results of global analysis

Local analysis SAP2000			
$M_{1,Ed}$	$M_{2,Ed}$	$M_{3,Ed}$	$M_{4,Ed}$
[kNm]	[kNm]	[kNm]	[kNm]
139000	101000	105000	142000
$\varphi_1$	$\varphi_2$	$\varphi_3$	$\varphi_4$
[°]	[°]	[°]	[°]
6,82	170,58	197,30	347,34

Table 4: Acting bending moments on concrete core

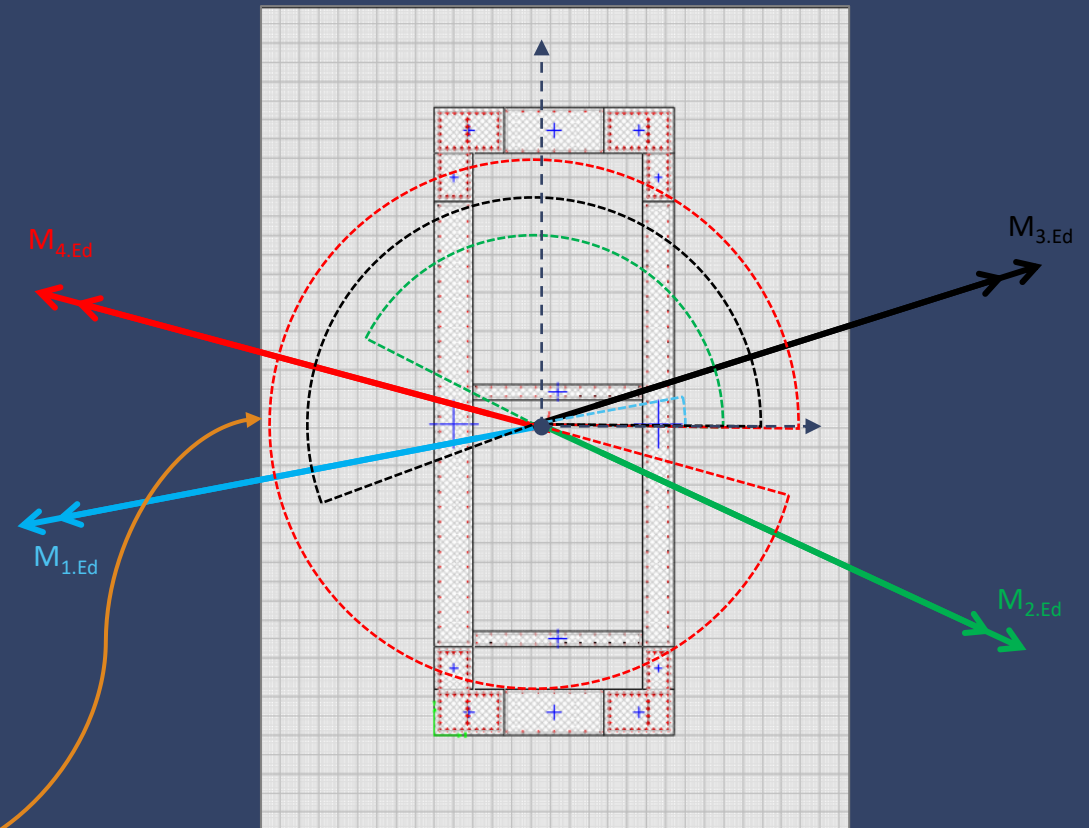


Figure 6: Resultant biaxial bending moments



## 2. Numerical example

### 2.2. Core wall as an integral element

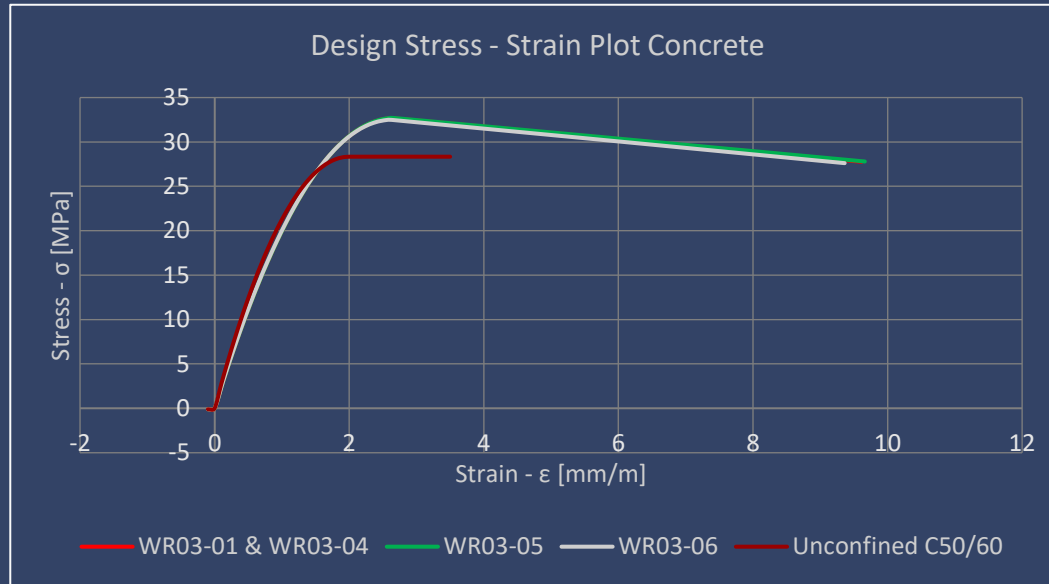


Figure 7: Concrete properties used in analysis

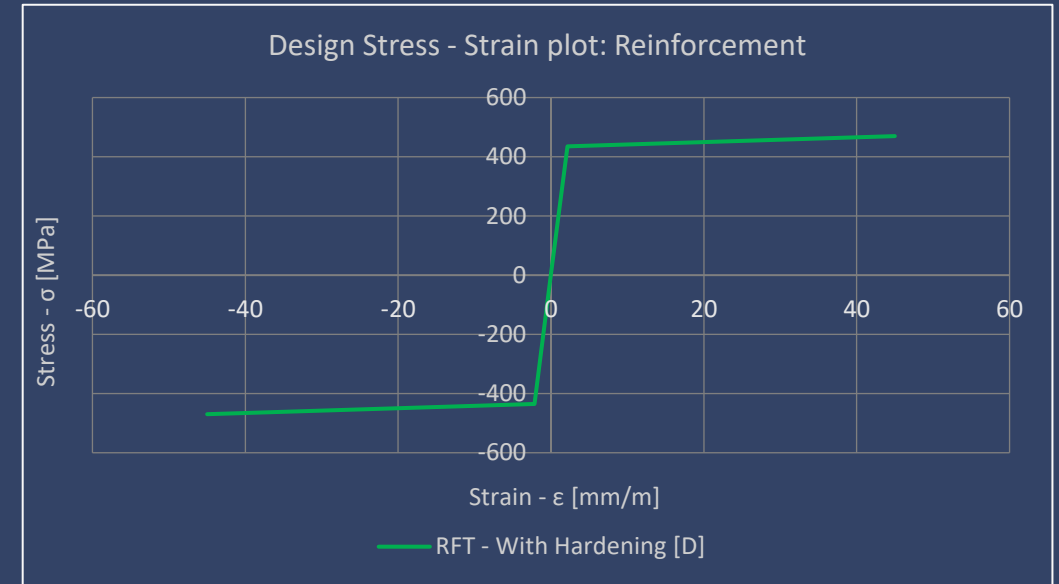


Figure 8: Reinforcement properties used in analysis



## 2. Numerical example

### 2.2.1. Core wall as an integral element – Curvature at the onset of yielding

- CSi SAP2000 v21.2.0 is used to monitor stresses and strains in section

Curvature ductility

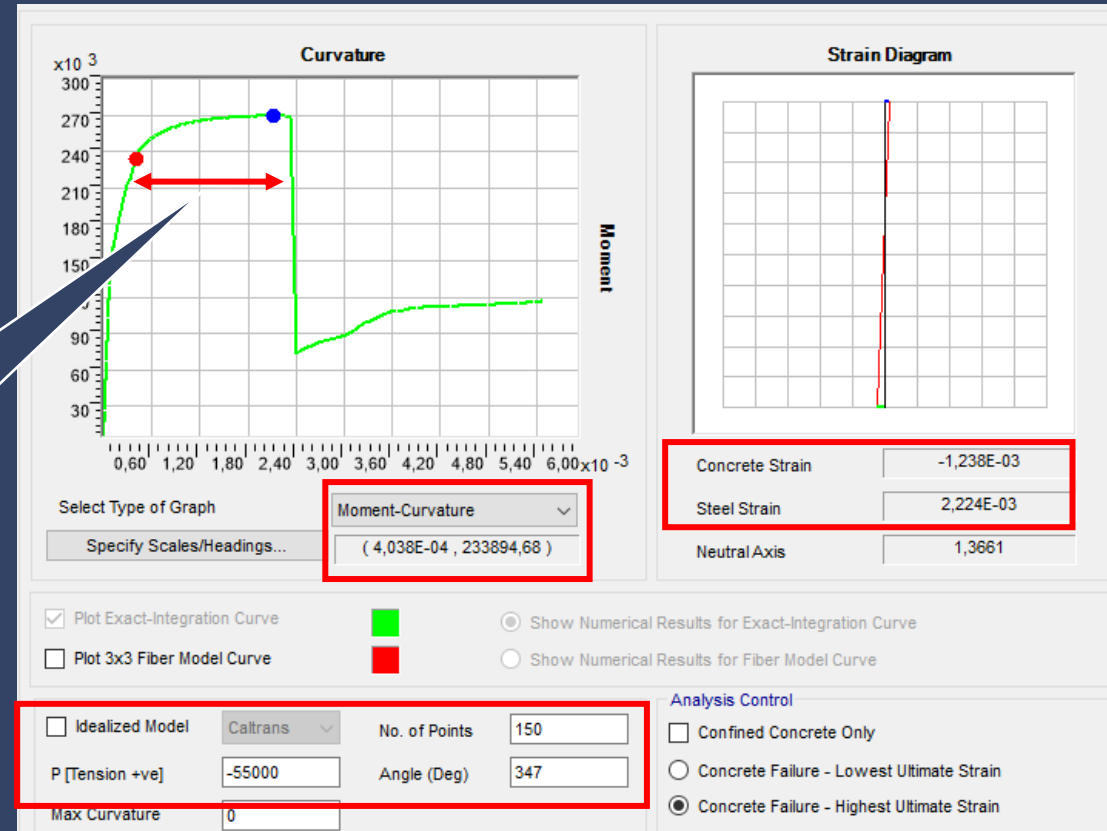


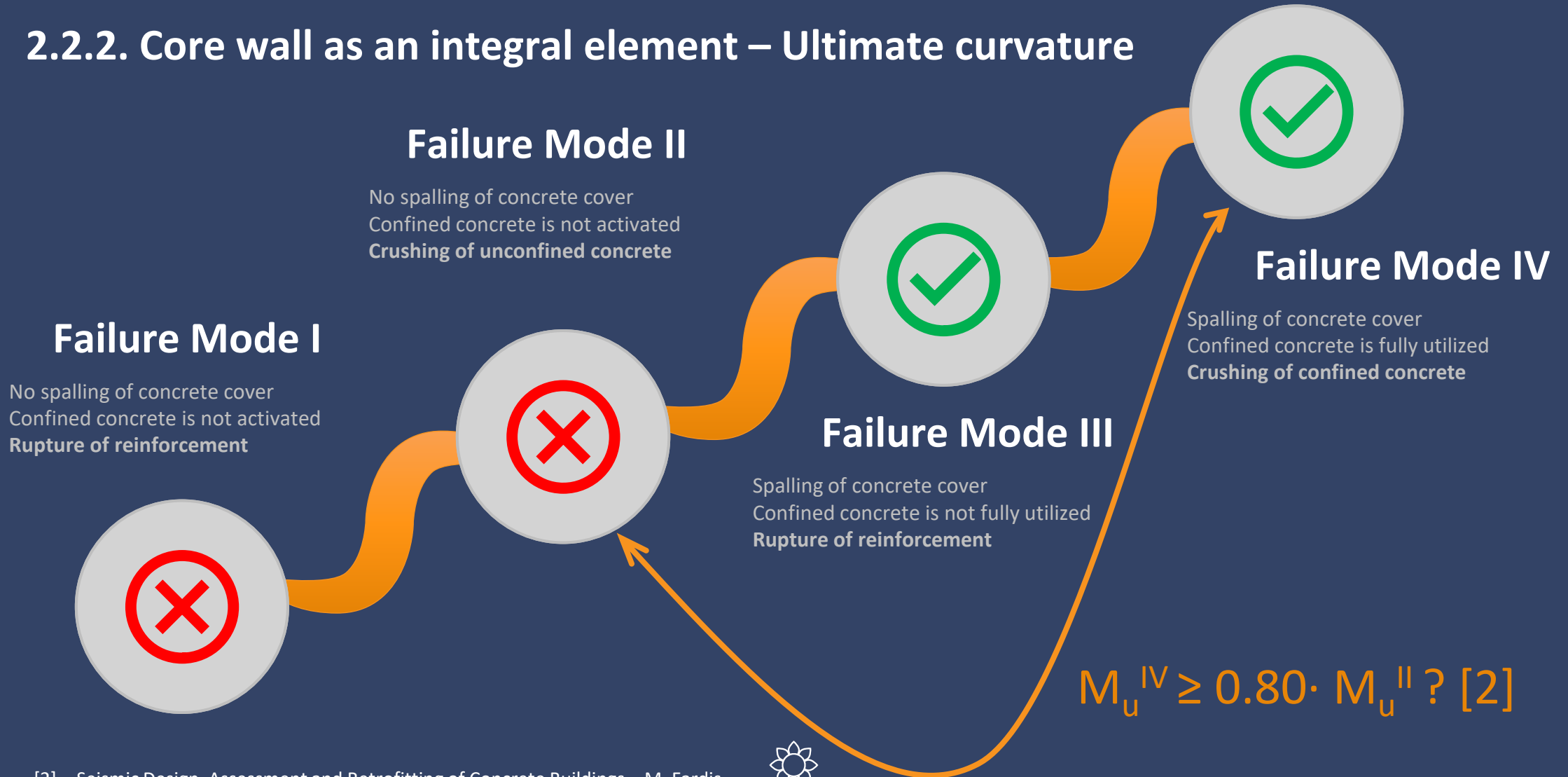
Figure 7: Moment – curvature diagram





## 2. Numerical example

### 2.2.2. Core wall as an integral element – Ultimate curvature



## 2. Numerical example

### 2.2.2. Core wall as an integral element – Ultimate curvature

- Necessary to determine does the section recover after spalling of concrete cover
- Verifications are performed on two separate section models

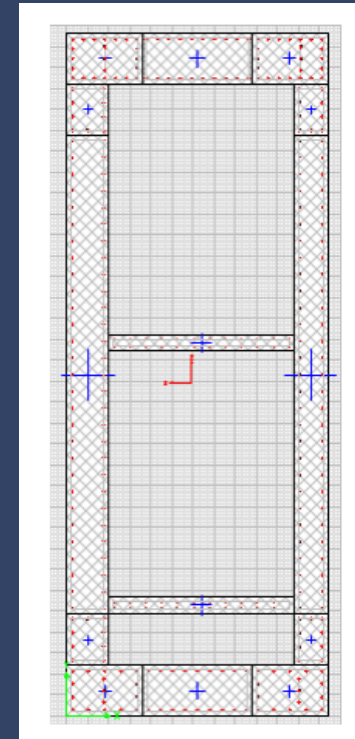


Figure 8: Section for failure modes I and II

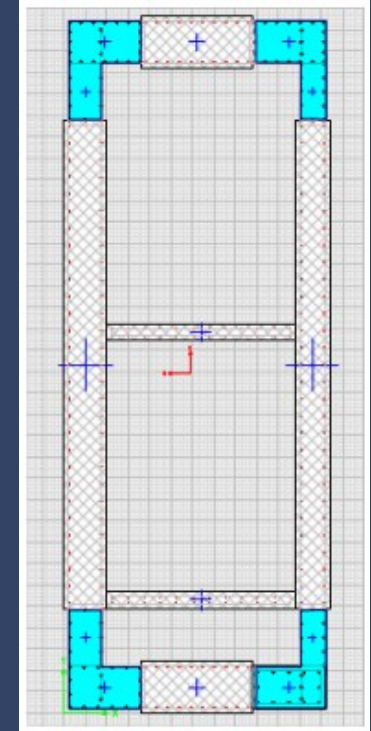


Figure 9: Section for failure modes III and IV



## 2. Numerical example

### 2.2.2. Core wall as an integral element – Ultimate curvature



Figure 10: Failure mode II (failure of unconfined concrete)

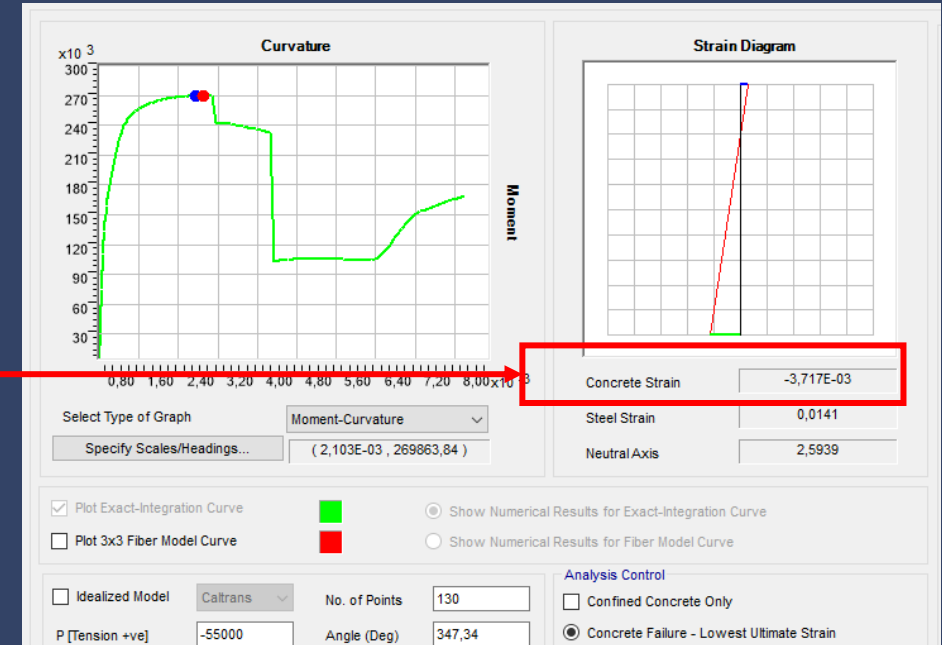


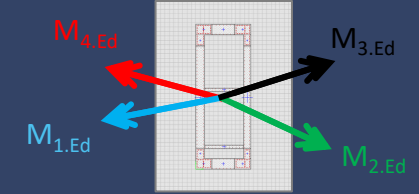
Figure 11: Failure mode IV (failure of confined concrete)

$$M_u^{IV} \geq 0,80 \cdot M_u^{II} ? \leftrightarrow 269\,863 \text{ kNm} \geq 0,80 \cdot 269\,926 \text{ kNm} \quad \checkmark$$



## 2. Numerical example

### 2.2.2. Core wall as an integral element – Ultimate curvature



$$\mu_{\phi.cap.4.s} = \frac{\mu_{u.4}^{IV}}{\mu_{y.4}} = \frac{2,189 \cdot 10^{-3} rad}{3,956 \cdot 10^{-4} rad} = 5,50$$

$$\mu_{\phi.req} = (2 \cdot 2 - 1) \cdot 1,5 = 4,5$$

$$U_{r.d.4.s} = \frac{\mu_{\phi.req}}{\mu_{\phi.cap.4}^{IV}} = \frac{4,50}{5,50} = 81,32\%$$

$$M_{U.4.s}^{IV} = 269\,863 \text{ kNm}$$

$$U_{r.b.4.s} = \frac{M_{Ed.4}}{M_{U.4}^{IV}} = \frac{142\,000 \text{ kNm}}{269\,863 \text{ kNm}} = 52,60\%$$

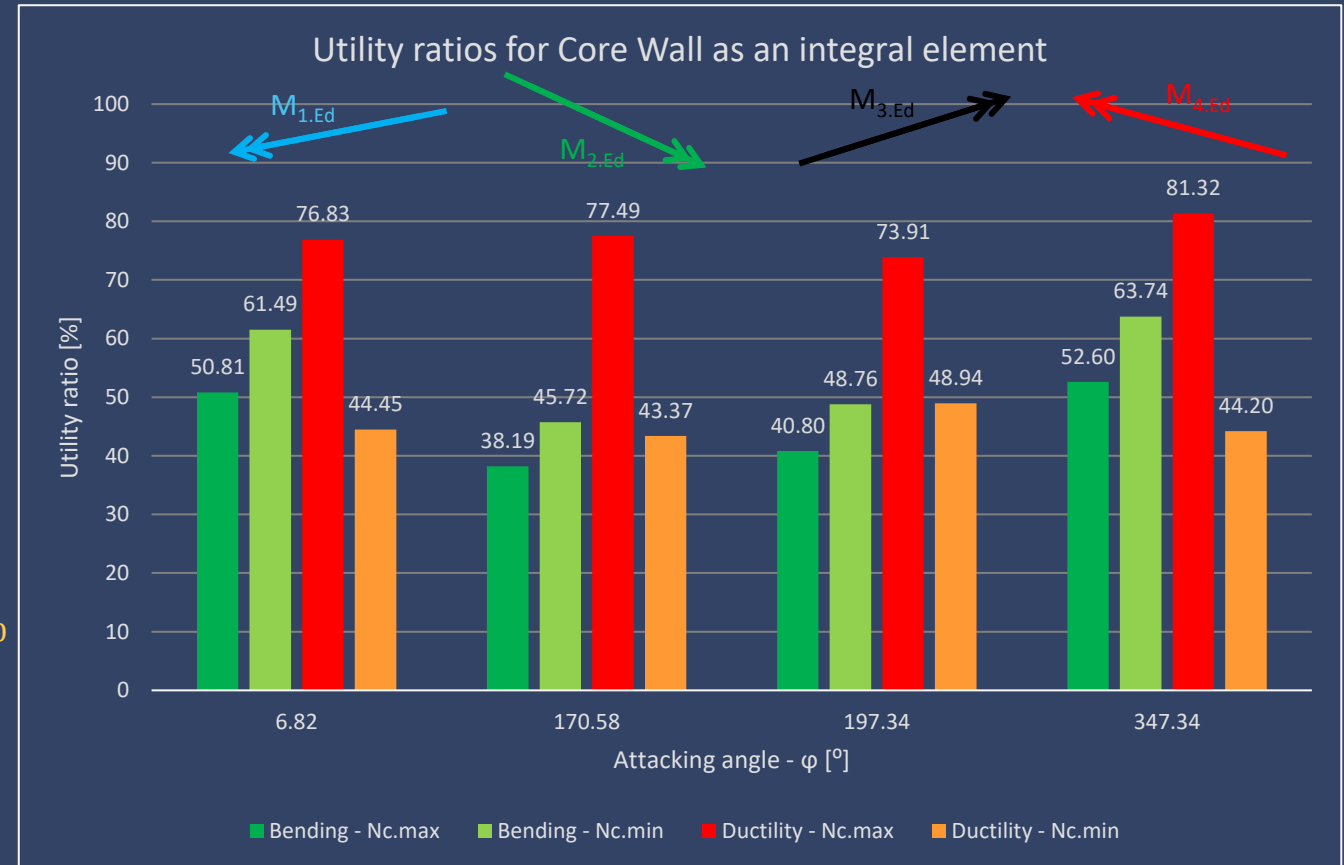


Figure 12: Summary of utility ratios for Core Wall as an integral element



## 2. Numerical example

### 2.2.3. Core wall as an integral element – Summary

- Do results differ from the analysis where constituent walls are treated analyzed independently?
- How efficiently confinement effects are utilized?
- Is this design the optimal one?



## 2. Numerical example

### 2.2.3.1. Integral section vs design of constituent sections independently?

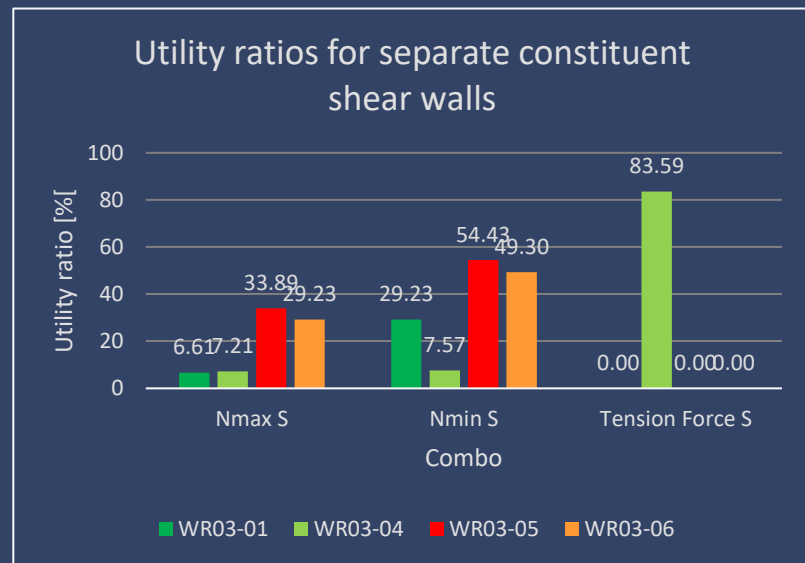


Figure 13: Summary of utility ratios for independent shear walls

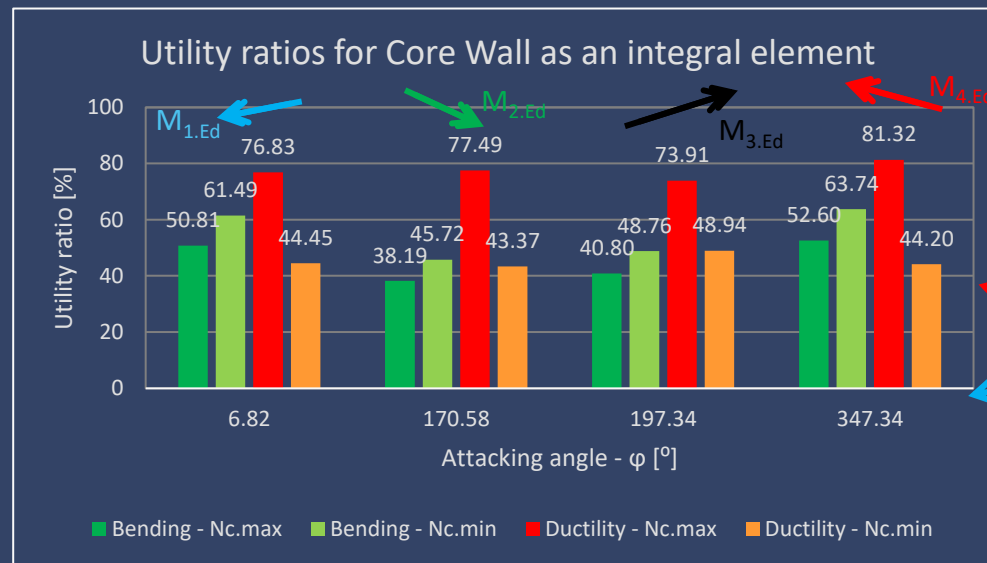


Figure 12: Summary of utility ratios for Core Wall as an integral element

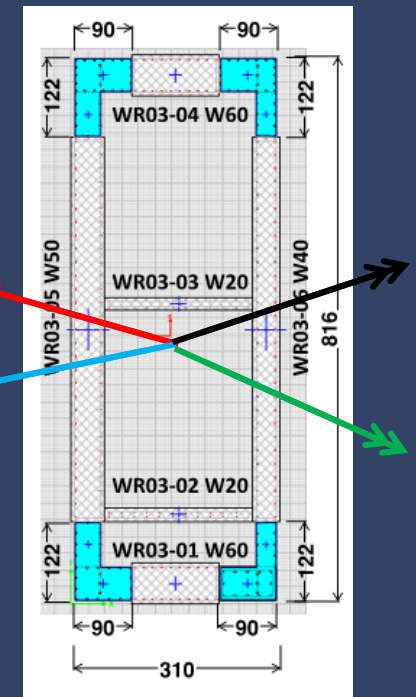


Figure 5: Confined zones and dimensions of core wall



## 2. Numerical example

### 2.2.3.1. Integral section vs design of constituent sections independently?



Figure 14: Utility ratio for independent shear wall WR03-01

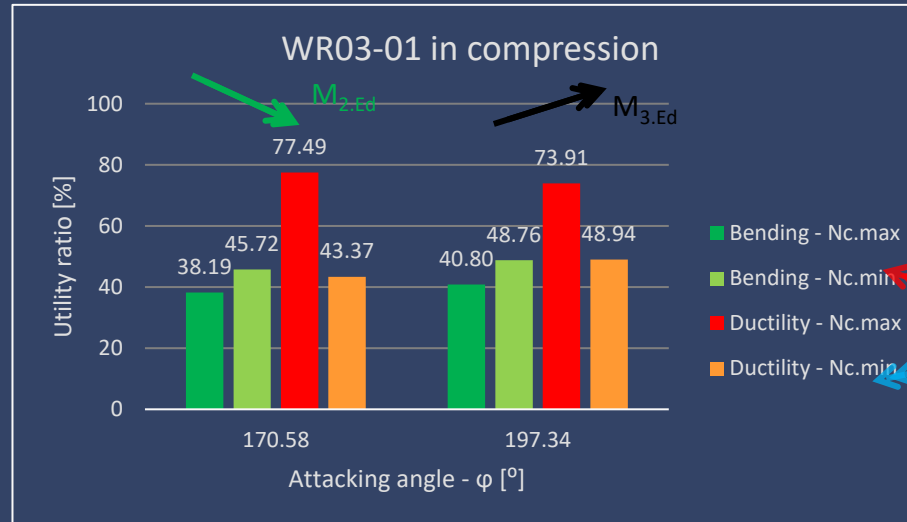


Figure 15: Utility ratios for resultant moments  $M_{2.Ed}$  and  $M_{3.Ed}$

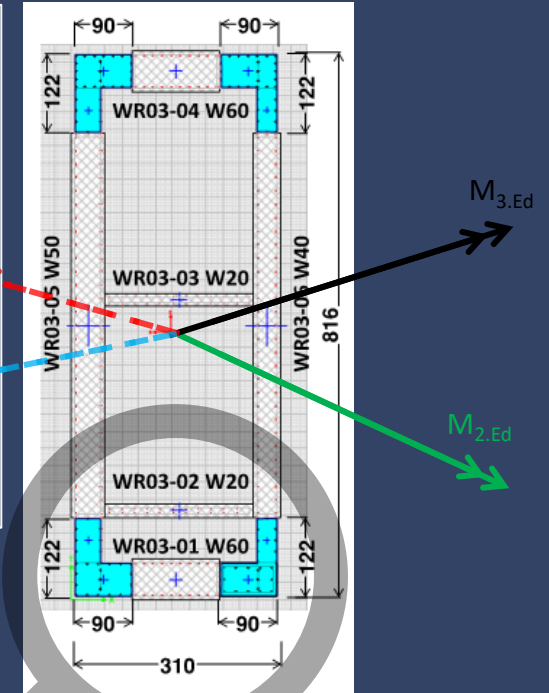


Figure 5: Confined zones and dimensions of core wall

Distribution of internal forces is vastly different if core wall is treated as an integral section!



## 2. Numerical example

### 2.2.3.2. How efficiently confinement effects are utilized?

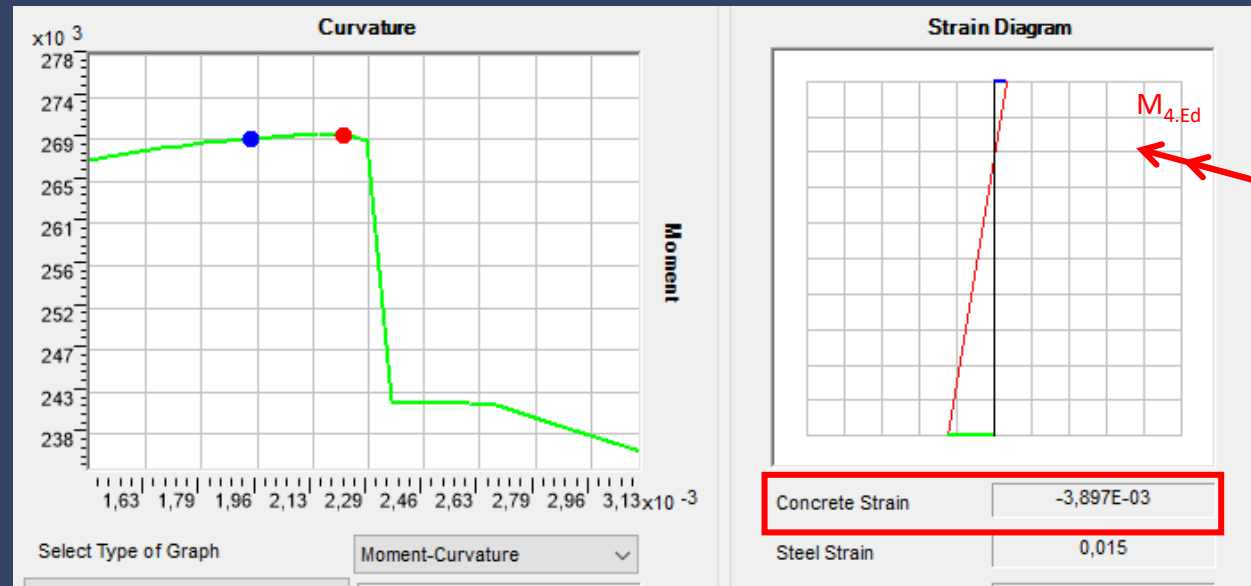


Figure 16: Moment-curvature plot for  $M_{4,Ed}$

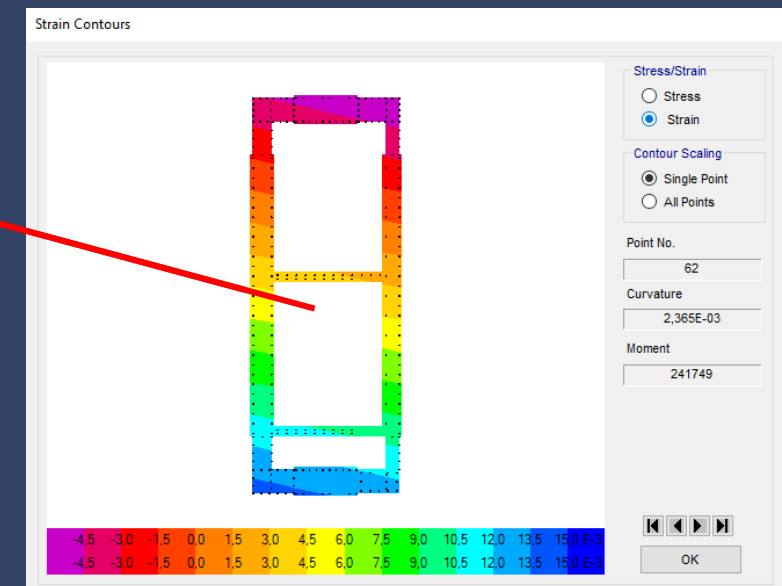


Figure 17: Strain distribution for  $M_{4,Ed}$





## 2. Numerical example

### 2.2.3.2. How efficiently confinement effects are utilized?

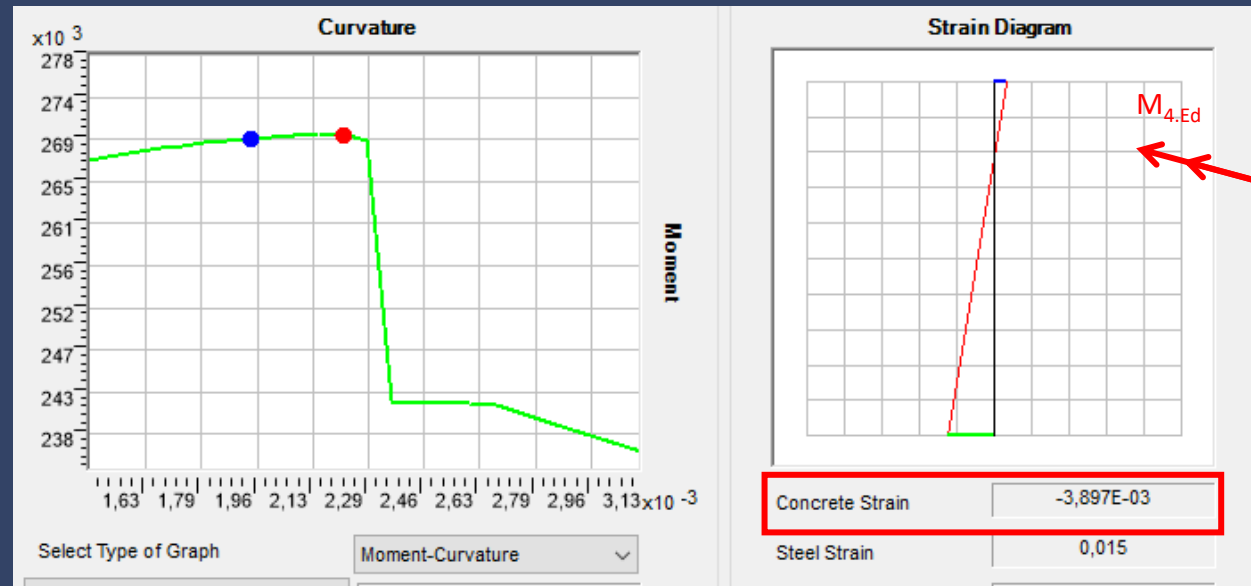


Figure 16: Moment-curvature plot for  $M_{4,Ed}$

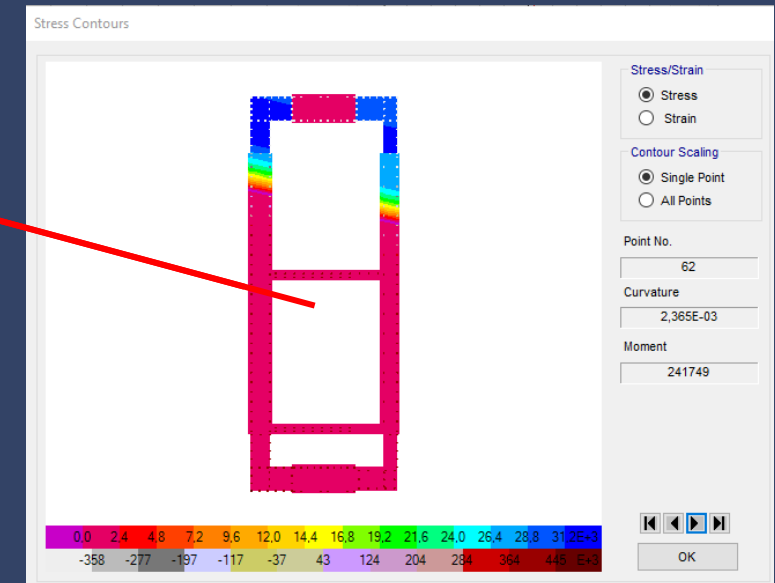


Figure 18: Stress distribution for  $M_{4,Ed}$



## 2. Numerical example

### 2.2.3.2. How efficiently confinement effects are utilized?

$$\varepsilon_{cu.c.ut} = 3,897 \cdot 10^{-3}$$

$$\varepsilon_{cu.c} = 9,362 \cdot 10^{-3}$$

$$U_{r,\varepsilon} = \frac{\varepsilon_{cu.c.ut}}{\varepsilon_{cu.c}} = \frac{3,897 \cdot 10^{-3}}{9,362 \cdot 10^{-3}} = 41,36\%$$

Poor use of confinement effects!

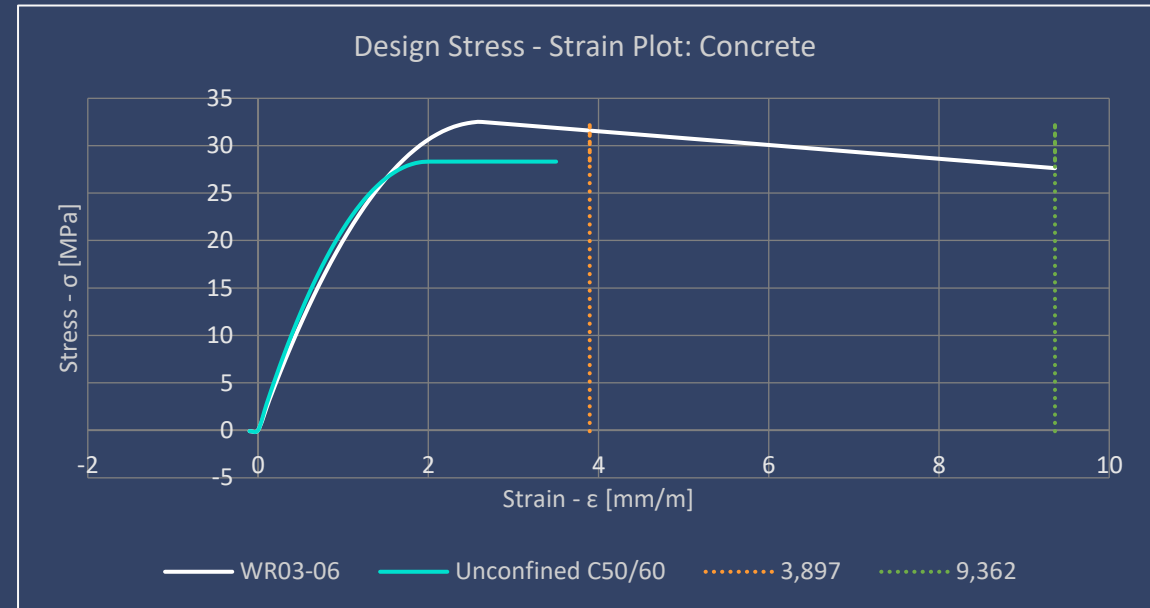
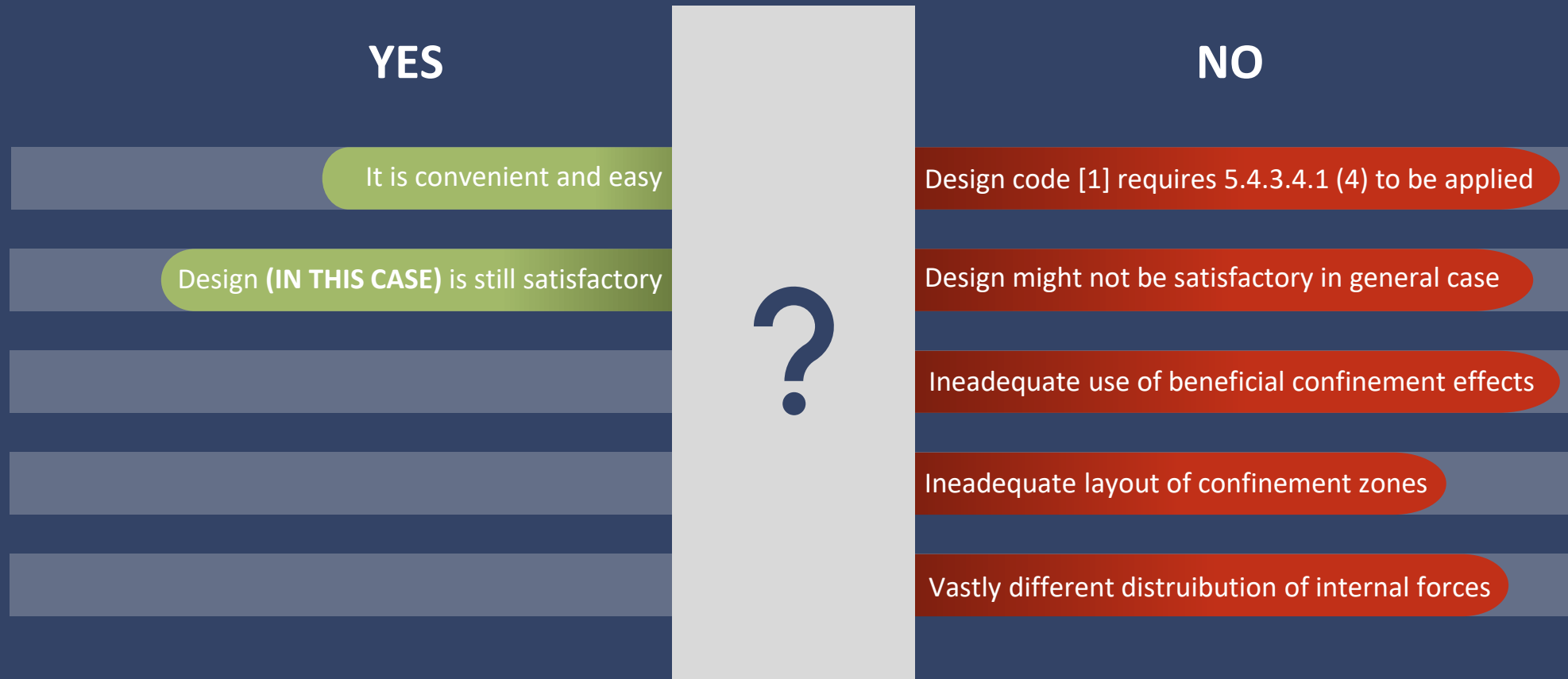


Figure 19: Utilization of confinement effects



## 2. Numerical example

### 2.2.3.3. Should constituent walls be treated as single shear walls?



# 3. Optimization

How to find optimized reinforcement layout?

Local analysis SAP2000			
$M_{1.Ed}$	$M_{2.Ed}$	$M_{3.Ed}$	$M_{4.Ed}$
[kNm]	[kNm]	[kNm]	[kNm]
139000	101000	105000	142000
$\varphi_1$	$\varphi_2$	$\varphi_3$	$\varphi_4$
[°]	[°]	[°]	[°]
6,82	170,58	197,30	347,34
$\Delta$			
±6,82	±9,42	±17,3	±12,66

Table 4: Acting bending moments on concrete core

Almost uniaxial bending of concrete core

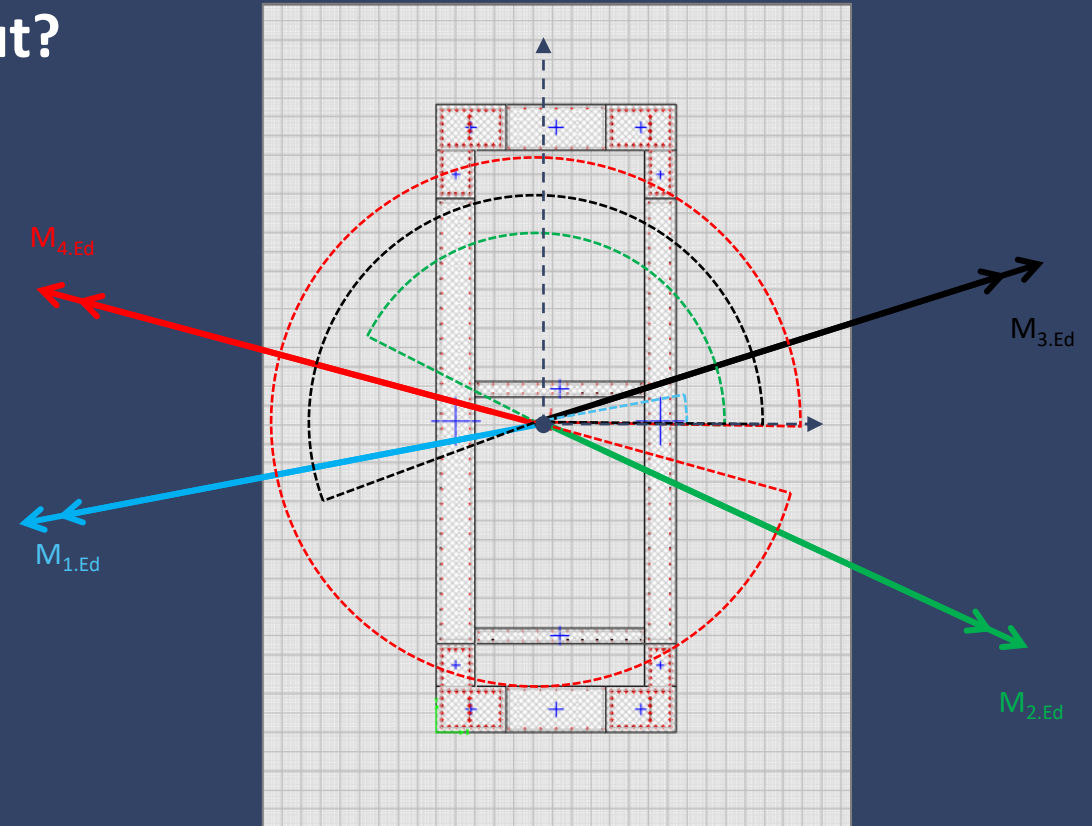


Figure 6: Resultant biaxial bending moments



# 3. Optimization

Analogy with single shear wall:

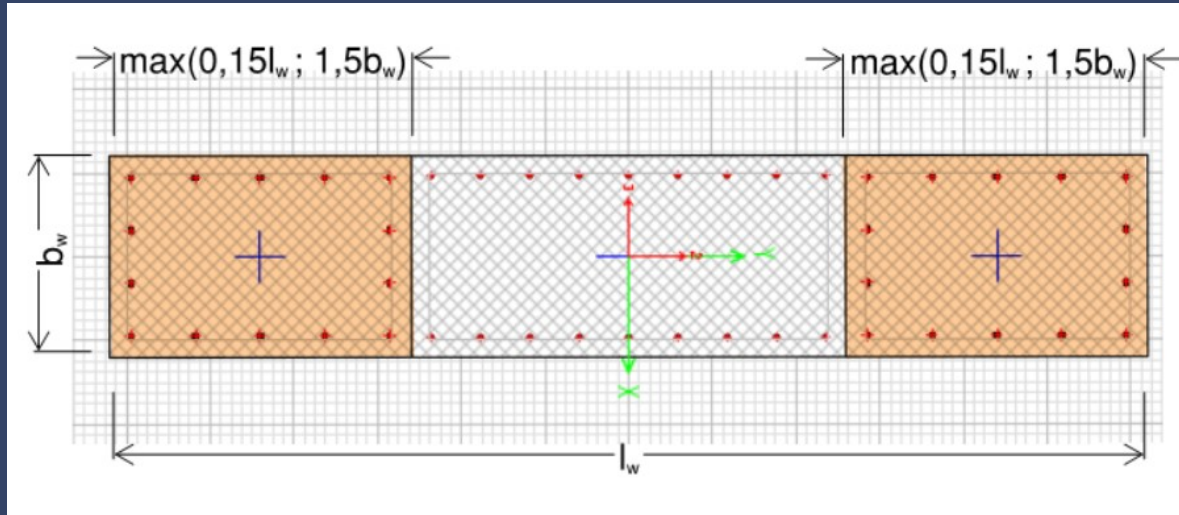


Figure 20: Minimal confined areas for single shear wall

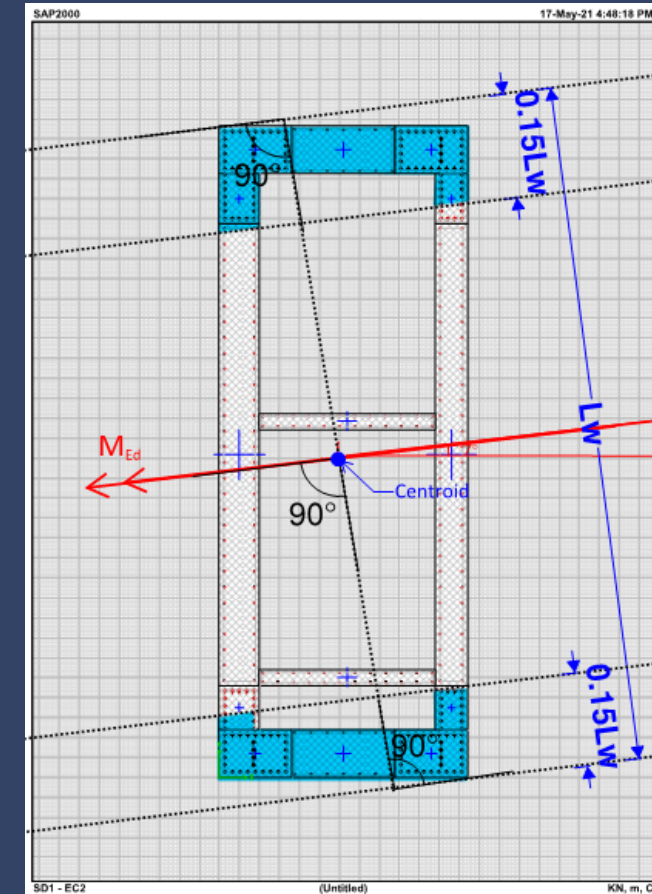


Figure 21: Proposed new layout of confined zones



### 3. Optimization

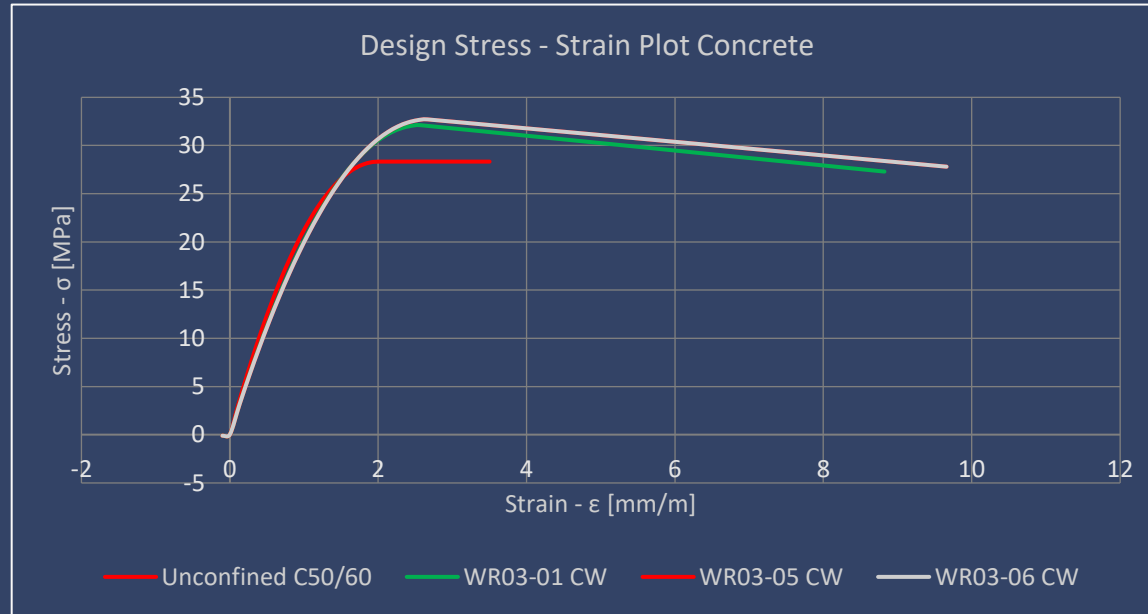


Figure 22: Updated confined concrete properties

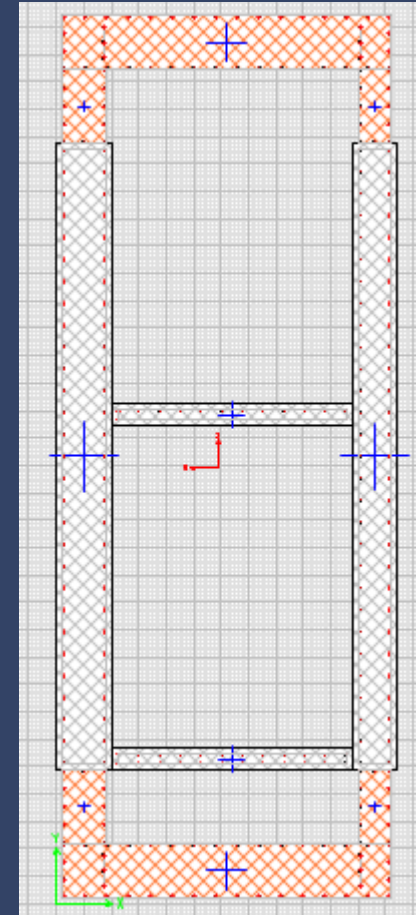


Figure 23: New layout of confined zones



# 3. Optimization

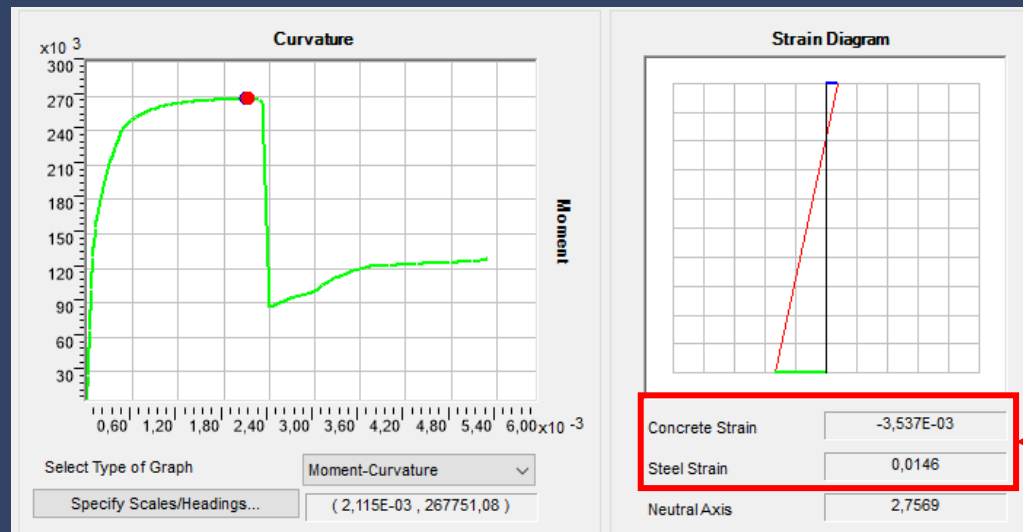


Figure 24: Failure mode II (failure of unconfined concrete)

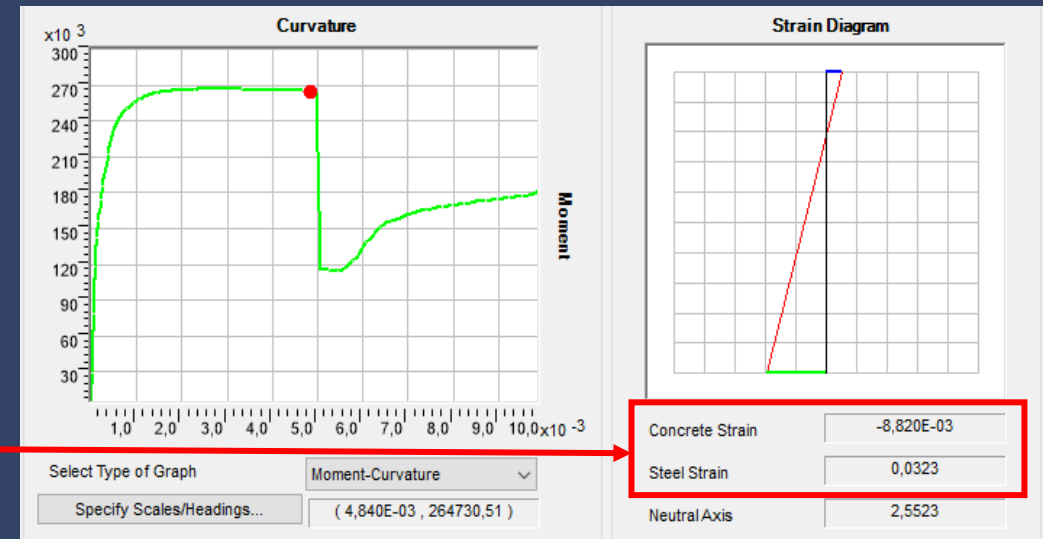


Figure 25: Failure mode IV (failure of confined concrete)

$$M_u^{IV} \geq 0,80 \cdot M_u^{II} ? \leftrightarrow 267\,430 \text{ kNm} \geq 0,80 \cdot 267\,751 \text{ kNm} \quad \checkmark$$



### 3. Optimization

$$\mu_{\phi.cap.4.r} = \frac{\mu_{u.4}^{IV}}{\mu_{y.4}} = \frac{4,840 \cdot 10^{-3} rad}{3,846 \cdot 10^{-4} rad} = 12,58$$

$$\mu_{\phi.req} = (2 \cdot 2 - 1) \cdot 1,5 = 4,5$$

$$U_{r.d.4.r} = \frac{\mu_{\phi.req}}{\mu_{\phi.cap.4}^{IV}} = \frac{4,50}{12,58} = 35,77\%$$

$$M_{U.4.r}^{IV} = 264\,728 \text{ kNm}$$

$$U_{r.b.4,r} = \frac{M_{Ed.4}}{M_{U.4}^{IV}} = \frac{142\,000 \text{ kNm}}{264\,728 \text{ kNm}} = 53,64\%$$

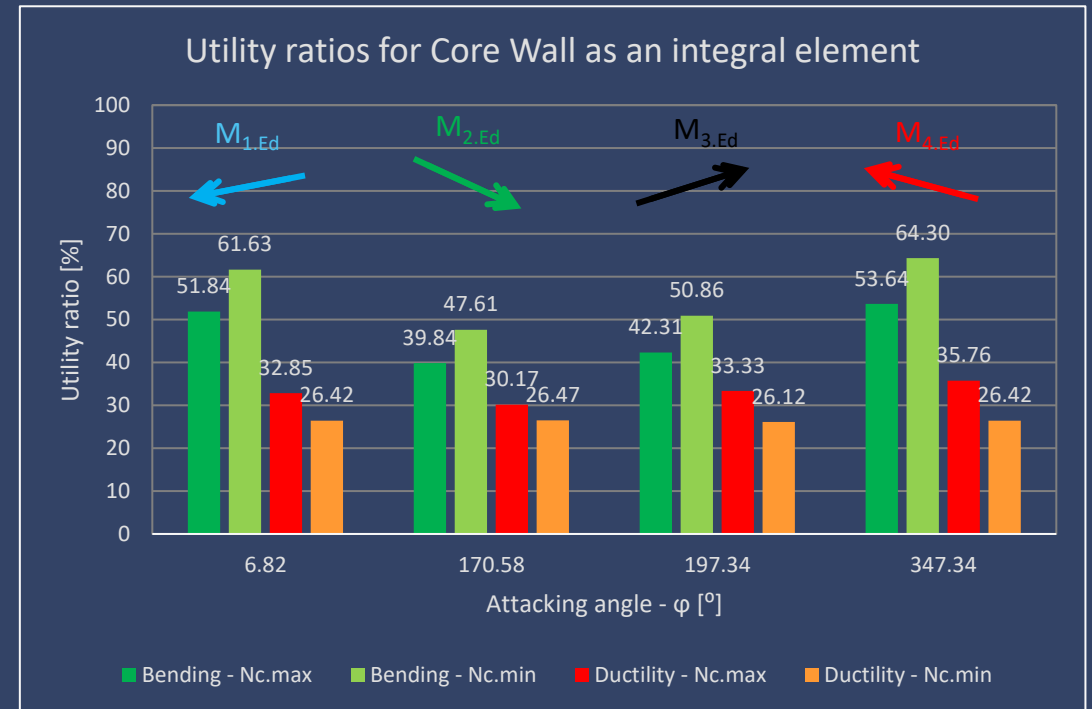
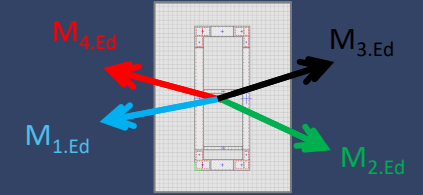


Figure 26: Summary of utility ratios for Core Wall as an integral element (revised layout)





### 3. Optimization

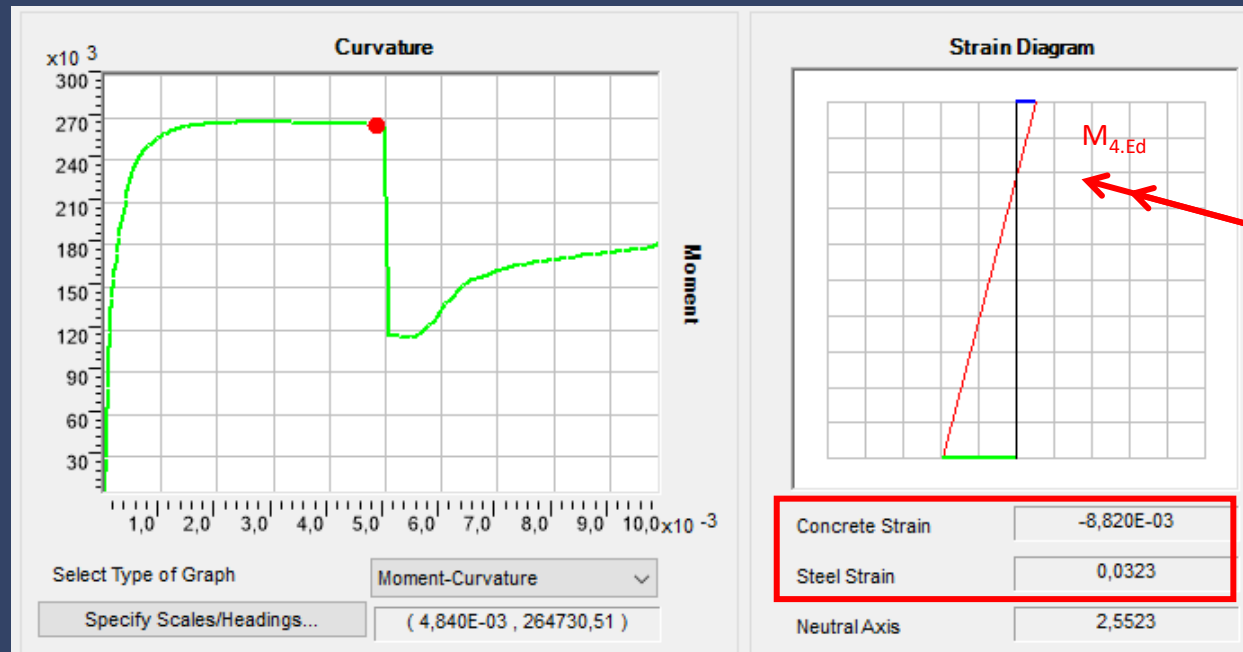


Figure 27: Moment-curvature plot for  $M_{4,Ed}$

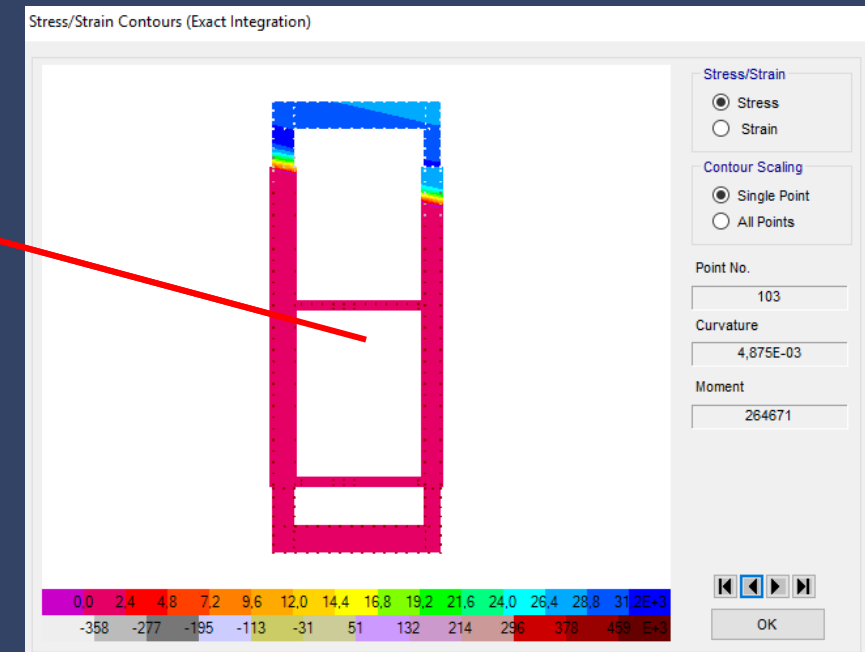


Figure 28: Stress distribution for  $M_{4,Ed}$



# 3. Optimization

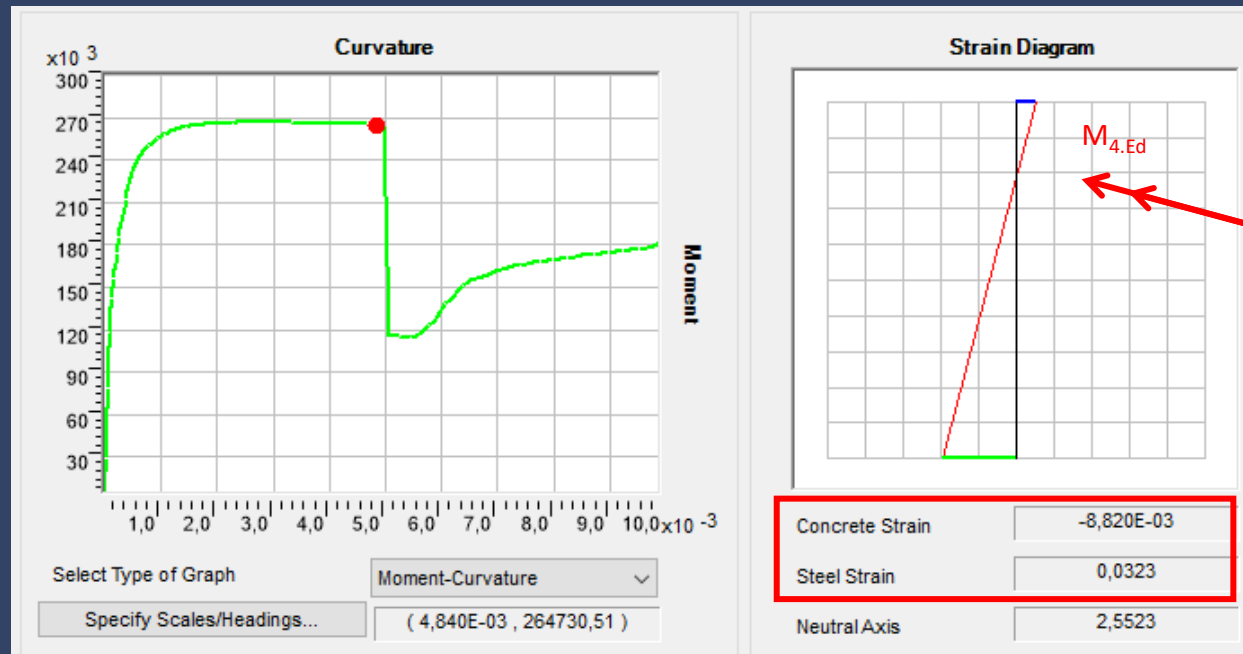


Figure 29: Moment-curvature plot for  $M_{4,Ed}$

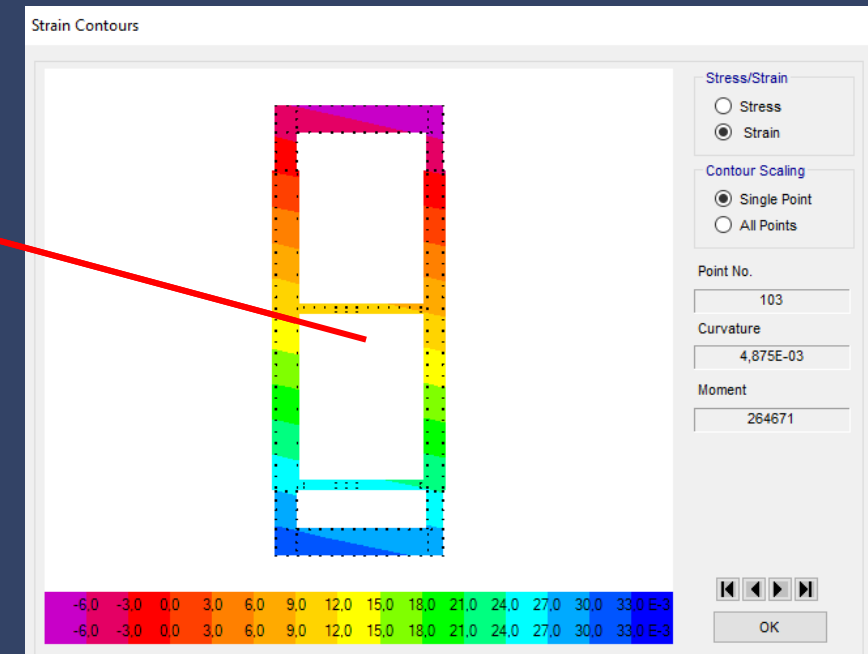


Figure 30: Strain distribution for  $M_{4,Ed}$



# 3. Optimization

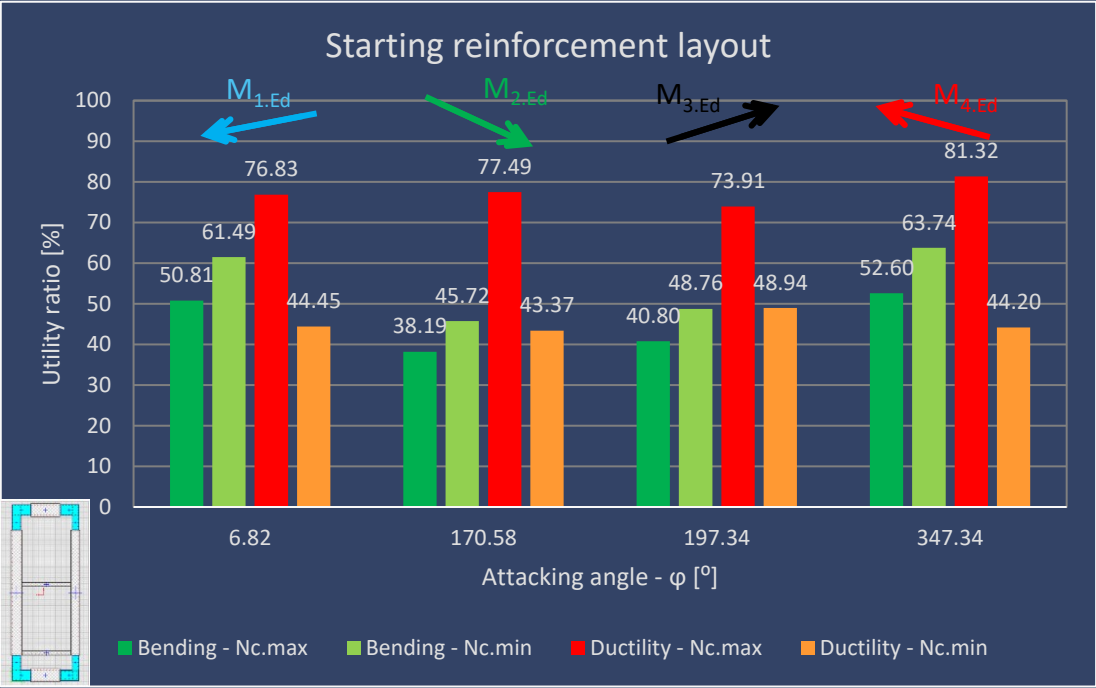


Figure 12: Summary of utility ratios for Core Wall as an integral element (starting layout)

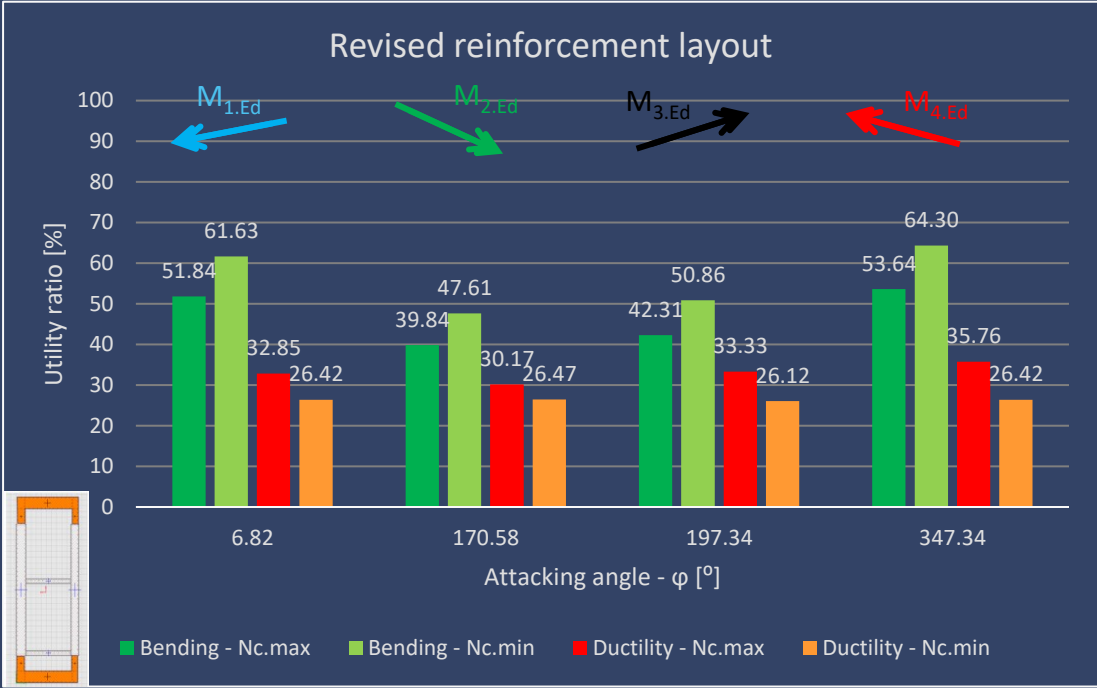


Figure 26: Summary of utility ratios for Core Wall as an integral element (revised layout)



# 3. Optimization

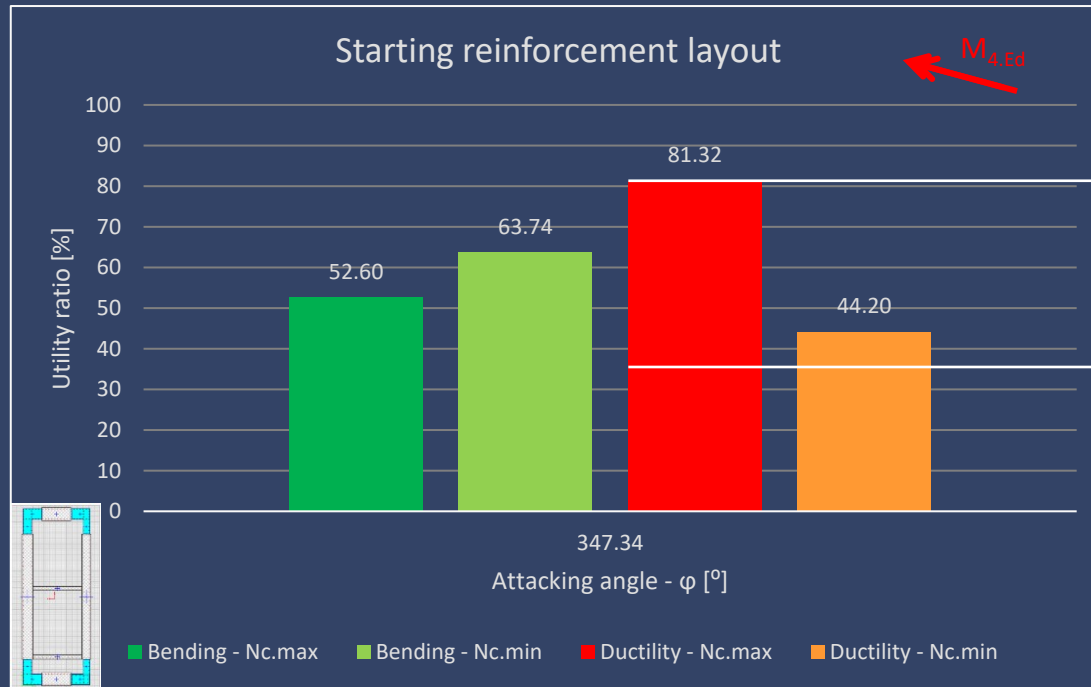


Figure 31: Utility ratios for Core Wall as an integral element (starting layout) –  $M_{4.Ed}$

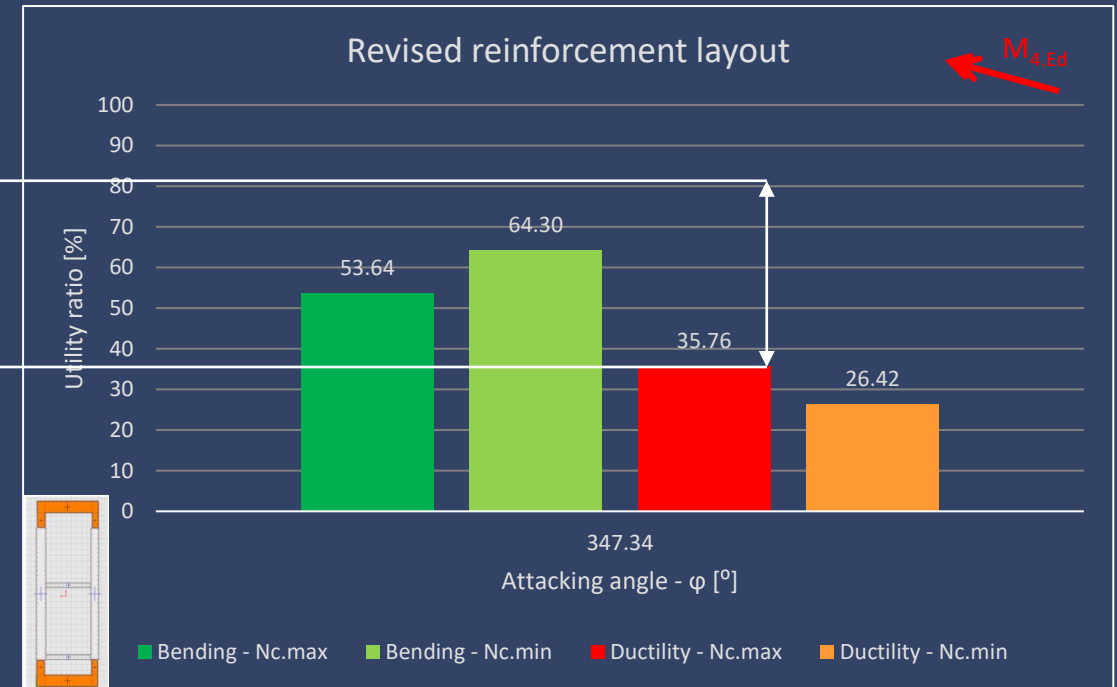
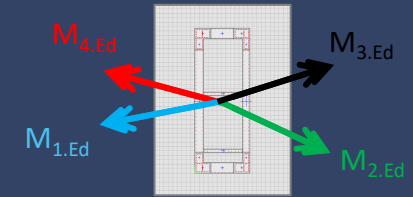


Figure 32: Utility ratios for Core Wall as an integral element (revised layout) -  $M_{4.Ed}$



# 3. Optimization

At what expense this improvement in behaviour is achieved?

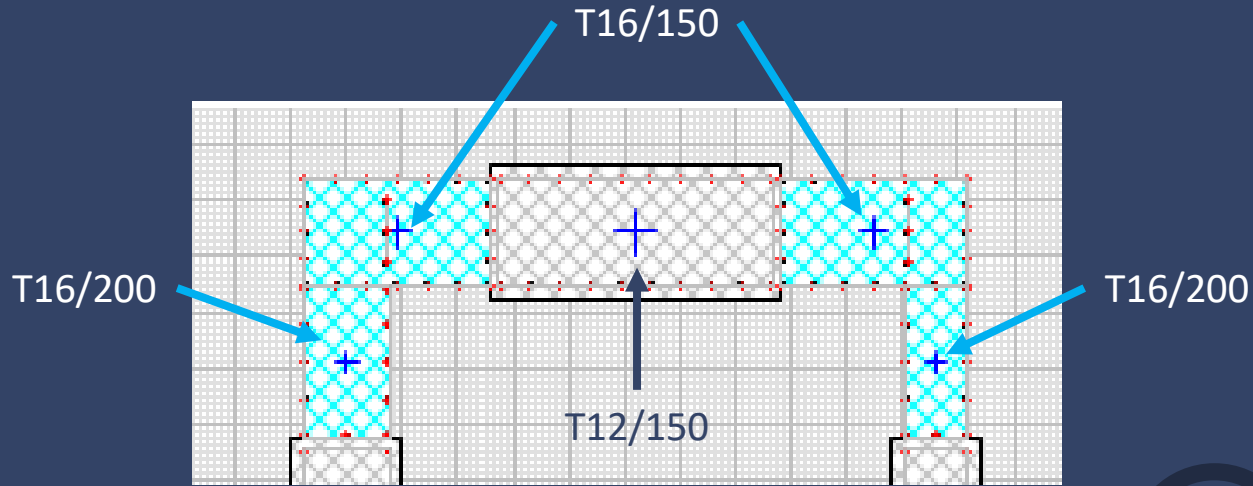


Figure 33: Starting layout of reinforcement

$$A_{s_s} = 65T12 + 20T12 = 153,31cm^2$$

$$\Delta_A = \frac{A_{s_r}}{A_{s_s}} = \frac{128,68cm^2}{153,31cm^2} = 83,93\%$$

$$\delta_A = \Delta_A - 1 = -16,07\%$$

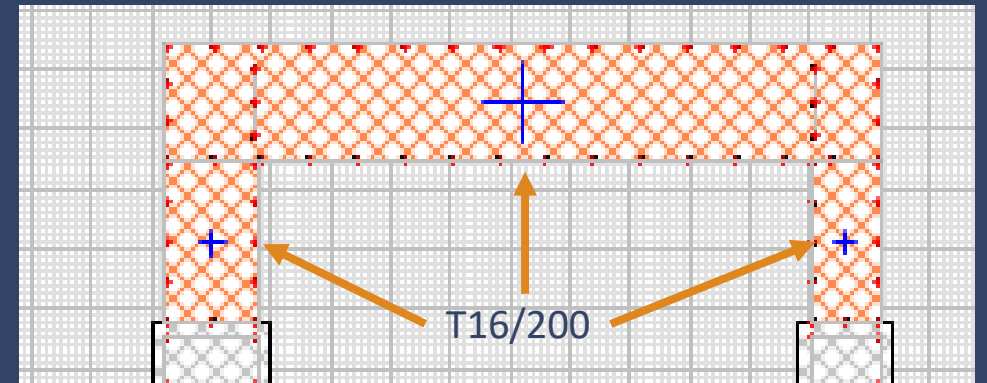
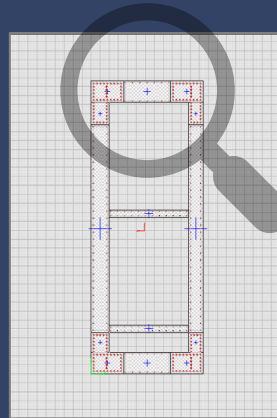


Figure 34: Revised layout of reinforcement

$$A_{s_r} = 64T16 = 128,68cm^2$$

$$\Delta_\mu = \frac{\mu_{\phi.cap.4.r}}{\mu_{\phi.cap.4.s}} = \frac{12,58}{5,50} = 228,73\%$$

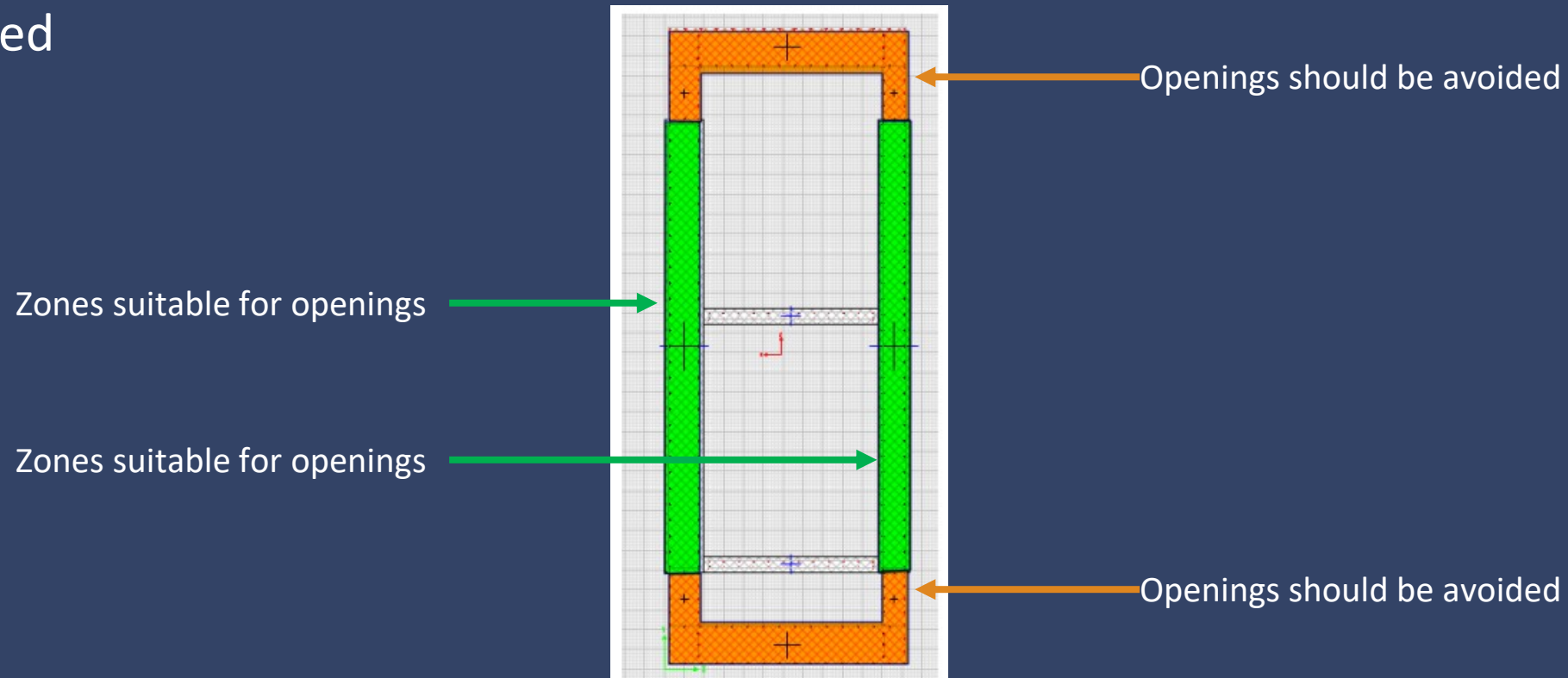
$$\delta_\mu = \Delta_\mu - 1 = 128,73\%$$



# 3. Optimization

## Special considerations - Openings?

- From the strain distribution it is easy to conclude which areas are most highly utilized



# 3. Optimization

## Special considerations - Openings?

5.2.1 (1) [1]



5.4.3.4.1 (4) [1]

5.4.3.4.2 (5) [1]

Summary

### Ductile wall:

Ductile wall is an element fixed at its base so that the relative rotation of this base with respect to the rest of the structural system is prevented, and that is designed and detailed to dissipate energy *in a flexural plastic hinge zone free of openings or large perforations, just above its base.*



# 3. Optimization

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## Special considerations - Openings?

*“...knowledge of their (composite walls) behavior under cyclic biaxial bending and shear is very limited, and that the rules used for their dimensioning and detailing still lack a sound basis... **Designers should opt for fairly simple geometries...**” [2]*

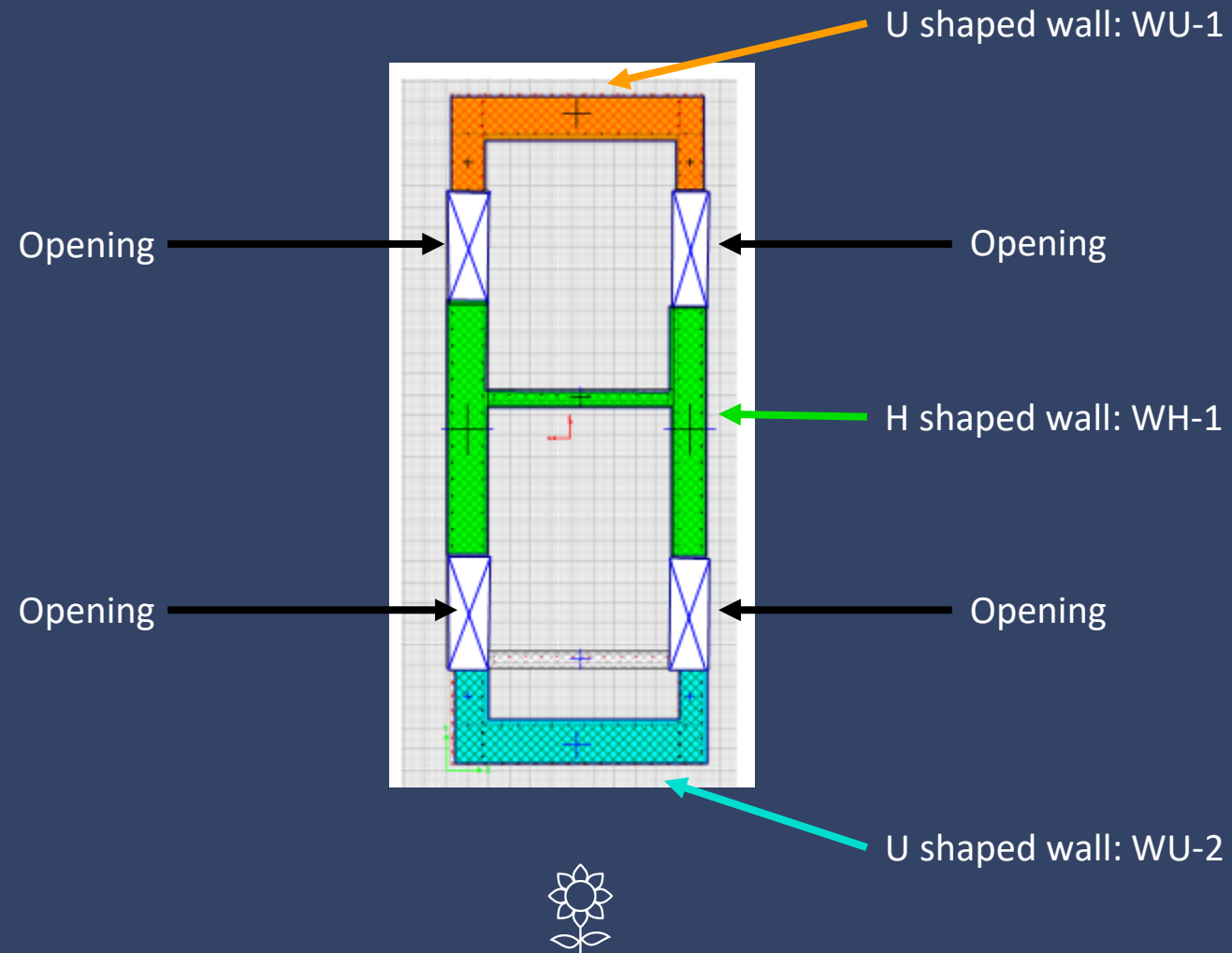
*“...**openings should be arranged at every floor at a very regular pattern**, turning the wall into a coupled one, with the lintels between the openings serving and designed as coupling beams...” [2]*





# 3. Optimization

## Special considerations - Openings?



## 4. Conclusions

---

1. Distribution of internal forces is vastly different if constituent walls are treated separately

*“...The nonlinearities in a section analysis at the ULS may lead to a distribution of strains and stresses in the actual composite section **which is vastly different from that in the artificially articulated section under the  $M_y$ - $M_z$ - $N$  triplets of its individual parts**. So, these triplets should be composed into a single one for the entire wall section..” [2]*



# 4. Conclusions

## 2. No correlation between behaviour of single shear walls and concrete core as an integral section

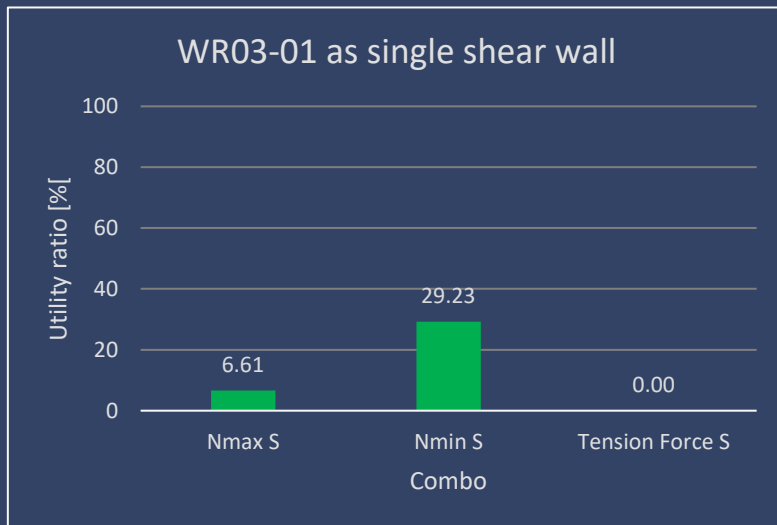


Figure 14: Utility ratio for independent shear wall WR03-01

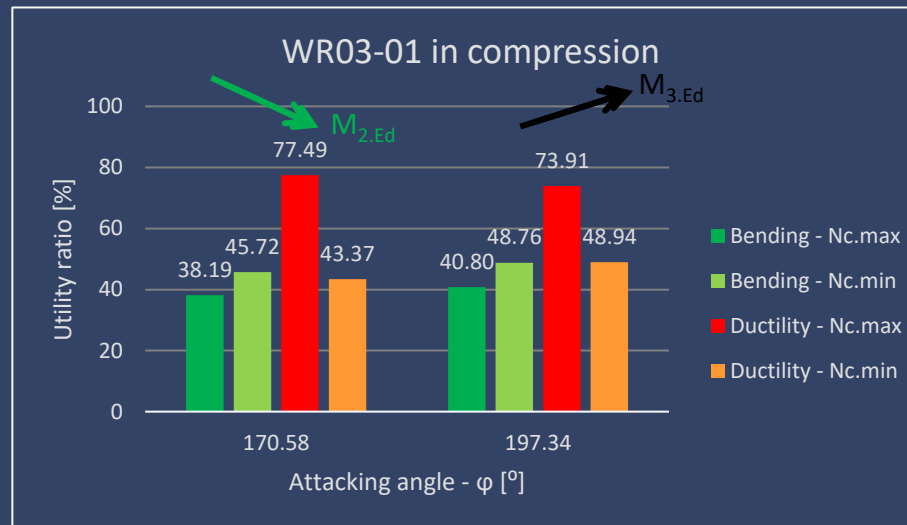


Figure 15: Utility ratios for resultant moments  $M_{2.Ed}$  and  $M_{3.Ed}$

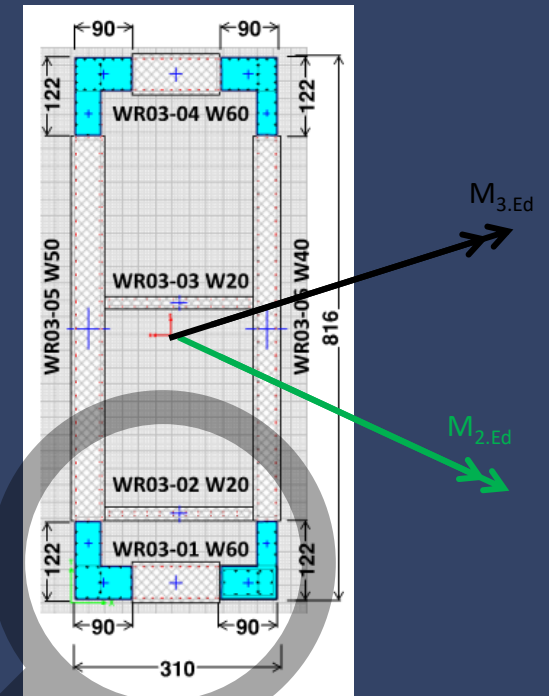


Figure 5: Confined zones and dimensions of core wall



# 4. Conclusions

3. There is no evidence to prove that design of constituent walls as single sheer walls is on safe side! **On the contrary it is probably not!!!**

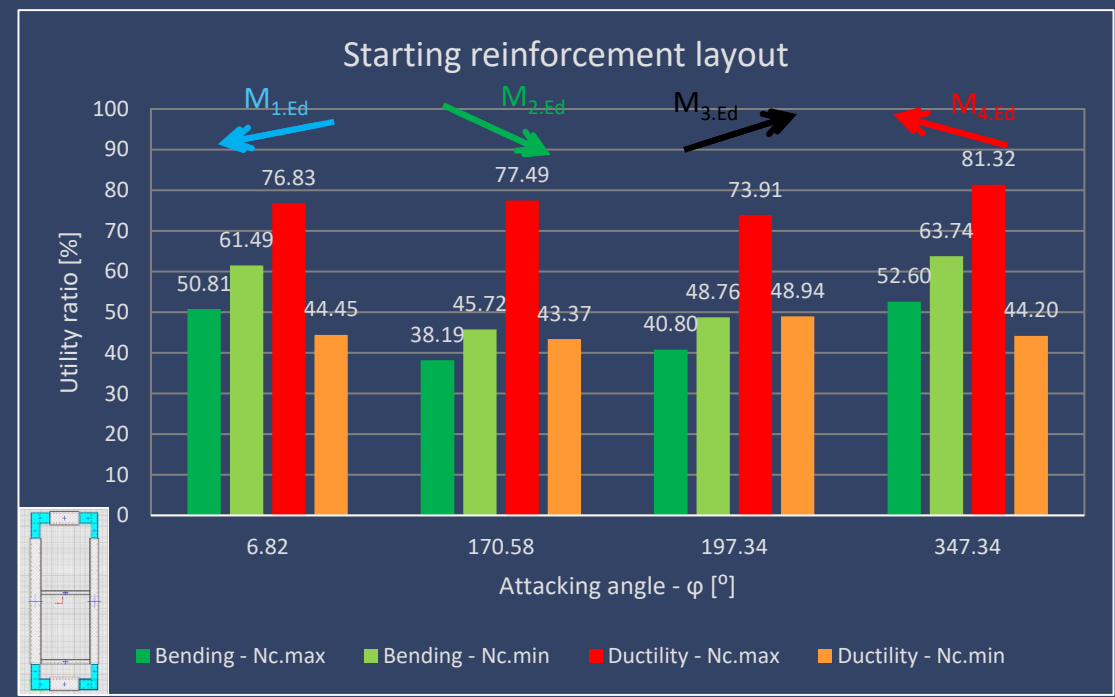
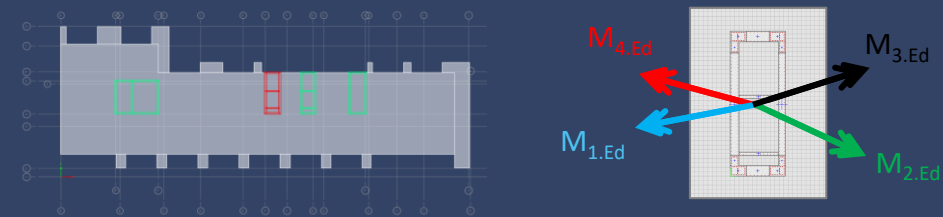


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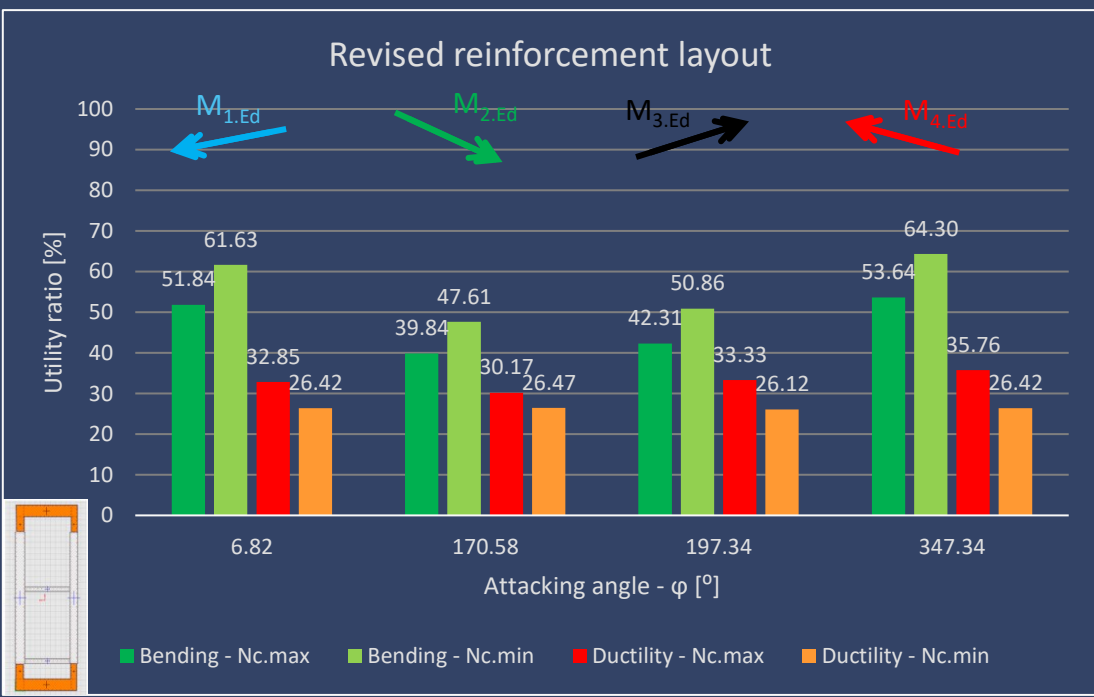


Figure 26: Summary of utility ratios for Core Wall as an integral element (revised layout)



